

Prof. Dr. Ir. Henri A. MASSON

**Analysis of complex systems and
associated signals (time series)**

Bijeenkomst over oorzaken van klimaatverandering

8 december 2012

Planetarium Museum/Johannes Post School
Rijksstraatweg 101, 2988 BB Ridderkerk–Rijsoord

Scope

- Limitation of linear analysis
- Some usual signal patterns and their signature
- An example of chaotic signals
- Advanced non linear signal analysis
- The Earth Climate case: analysis of temperature time series
- Predictability of Earth Climate

CLASSICAL ANALYSIS OF TIME SERIES & THEIR LIMITATIONS

Classical methods for time series analysis

- **Moving average**

$$X_{t+1} = \frac{1}{n} \sum_{i=0}^{n-1} \omega_i X_{t-i}$$

- **Exponential smoothing**

$$X_{t+1}^* \stackrel{\text{def}}{=} \alpha X_t + (1 - \alpha) X_t^*$$

α is a tuning parameter ($0 \leq \alpha \leq 1$)

X_t^* is the predicted value of the indicator X at time t

X_t is the actual value observed for the indicator X at time t

- **Regression (least squares)**

- Linear
- Polynomial
- Exponential, logarithmic, hyperbolic, etc.

- **Seasonal effects**

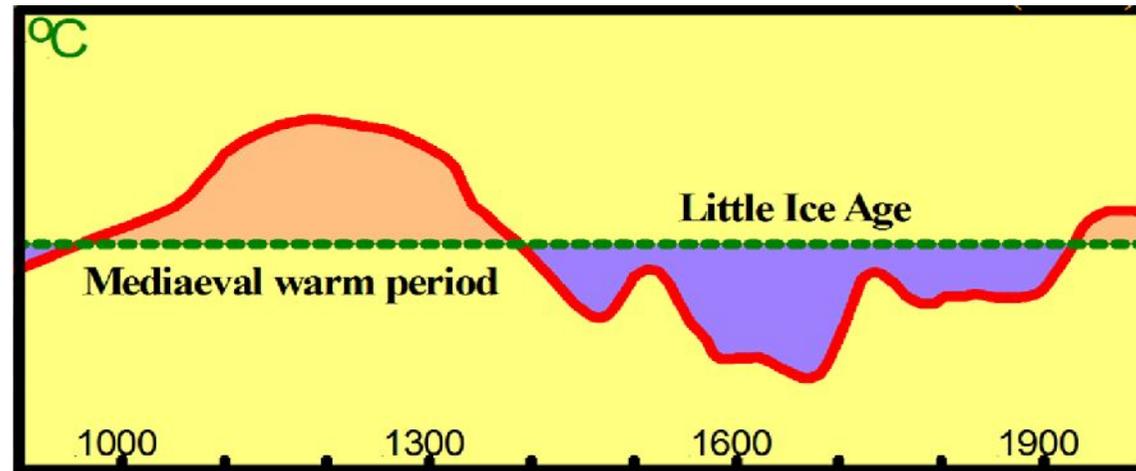
- **Factor analysis**

- variable Z (normal « reduced »)
- Co-variance matrix
- Eigen values and vectors (diagonalisation)
- Representation of reduced variables in this new axis system.

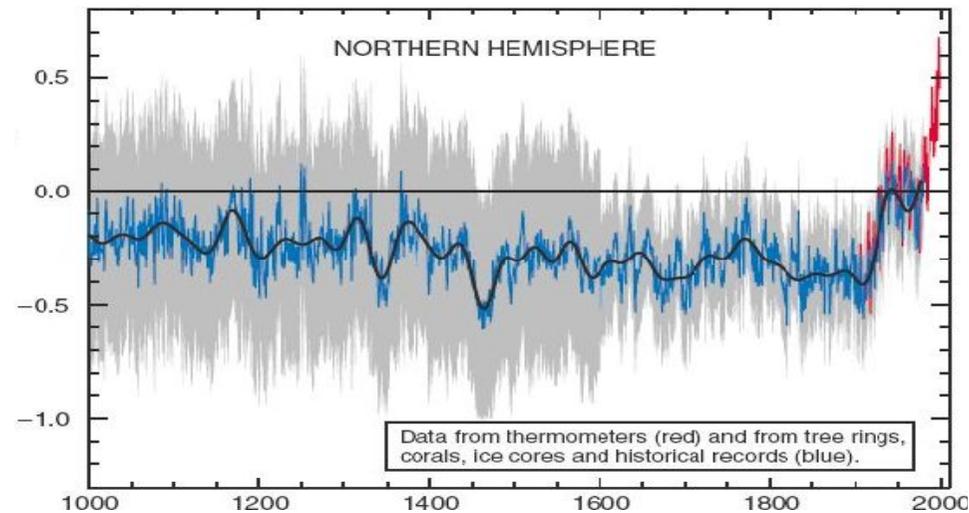
- **Hockey stick (Mann)**

- Higher confidence in recent measurements made by thermometers than by proxies
- Centering of variables on the mean value of most recent data only
- => **Error when calculating co-variance matrix (and eigen values + vectors)**
- => **bias** => hockey stick
- Random data generate also a hockey stick when submitted to the same treatment.

Which data to believe??



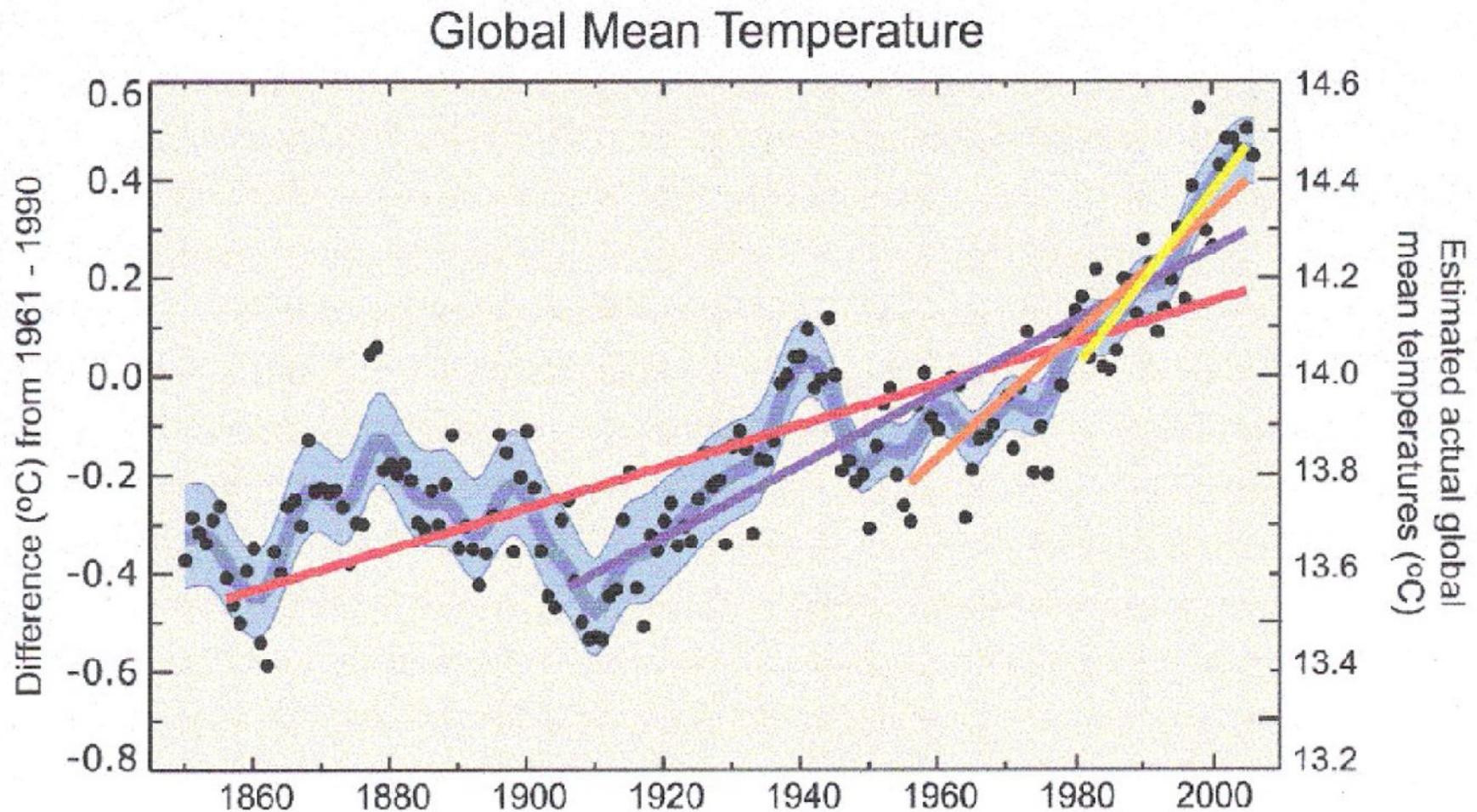
Original IPCC 1990 figure, confirmed by several recent experimental evidences (i.e; Bifra, 2009)



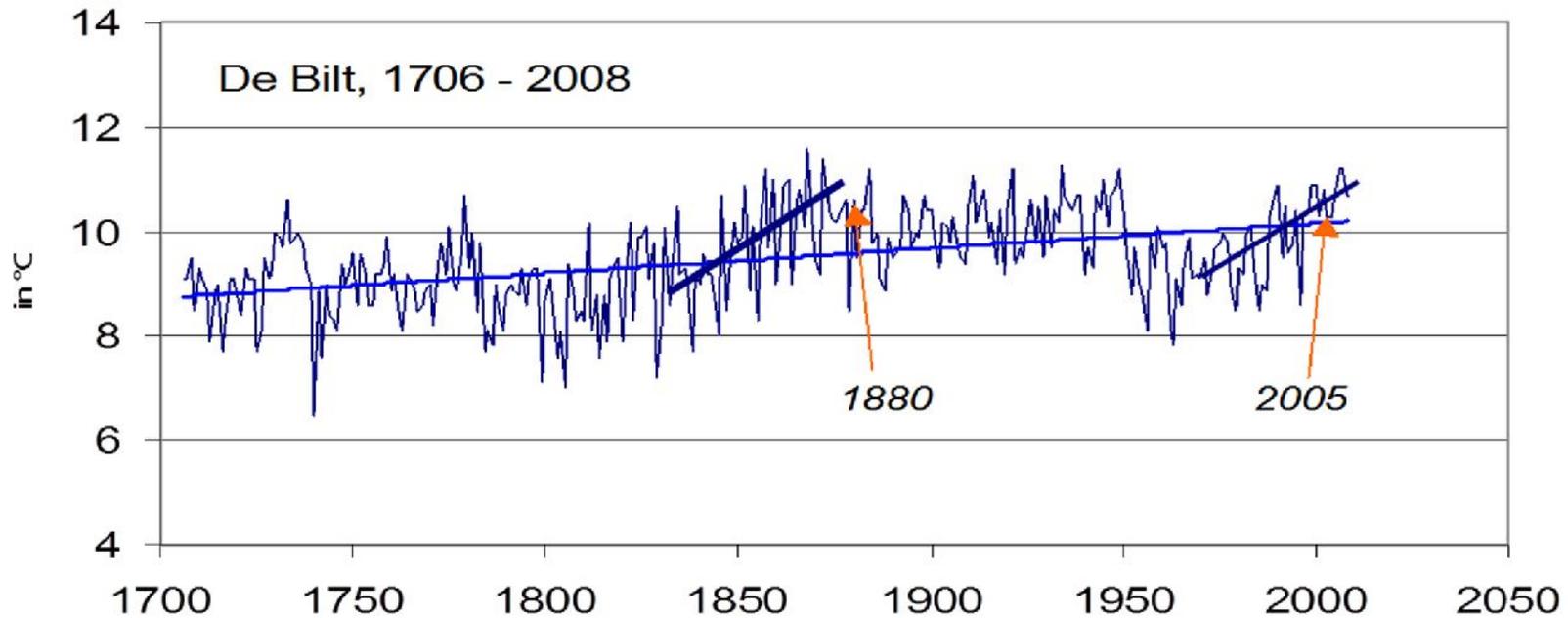
IPCC 2001 From M. Mann, the famous “hockey stick” curve!

IPCC 2007 & linear time series

Effect of the time window considered on the trend line

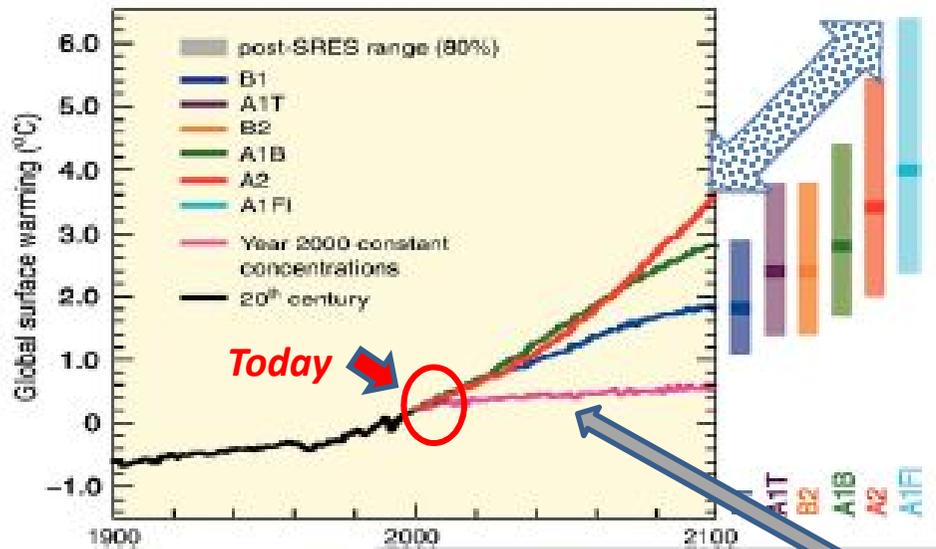


Is T° increasing faster those days than during early 19th century?



Evolution of the global temperature on Earth

IPCC MODELS PREDICTIONS



Key climate indicator for IPCC

Global temperature remains **constant** **since 16 years** (UK MET DBase Hadcrust 4, november 2012 update)

Cannot be explained by IPCC models (Rem: best fit so far: no increase in CO2 => no effect of CO2? => **flaw in model?**)

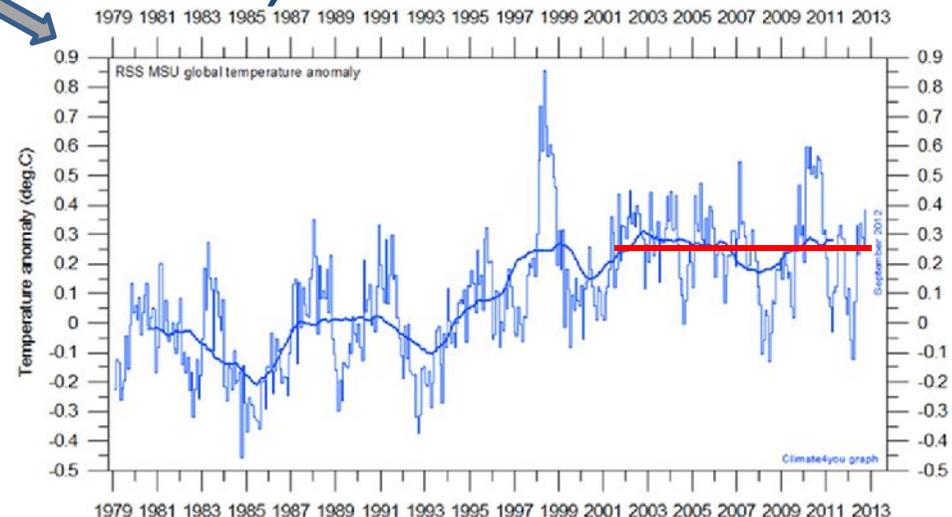
IPCC approach

Calibration over existing data (=> 1995)

After smoothing the data (by moving average) and **eliminating** « rogue points » (volcanoes eruptions, El Nino, etc.)

But periodic components are also **eliminated**.

What if natural cycles are significant?



**SOME EVIDENCES OF PERIODIC
COMPONENTS IN CLIMATIC DATA**

Oscillations in local temperature anomalies

Station	1710	1720	1730	1740	1750	1760	1770	1780	1790	1800	1810	1820	1830	1840	1850	1860	1870	1880	1890
Central England	0,045			0									0,036		0				-0,022
De Bilt		-0,0008														0,0606			-0,0065
Uppsala			-0,0287			0											-0,008		0,01
St.Petersburg					0						-0,07	0,09		-0,015					
Basel							-0,001												
Stockholm									0,041	-0,0076	0,12	-0,127	0,0354	0,0136					
Paris									-0,0024	0,0203			-0,0161						0
Mailand										0,0138		-0,0177							
Edinburgh										0,0163							-0,0107		
Kopenhagen										-0,01						0,0087			
Prag										0,0042									-0,0002
Wien										-0,002					0,0077				-0,0209
Vilnius										-0,002	0,056		0						
Warschau										-0,03			0,04		0				0
Budapest										0					0,0104		0		0
Hohenpeissenberg										0,0344		0,0071							0
München										0,062	-0,0081								0
Suttgart										-0,0903						0,11		-0,0587	
Breslau										0									0
Armagh											0,0013		0,0349						-0,0268
Roma													-0,0174			0,0405			-0,0019

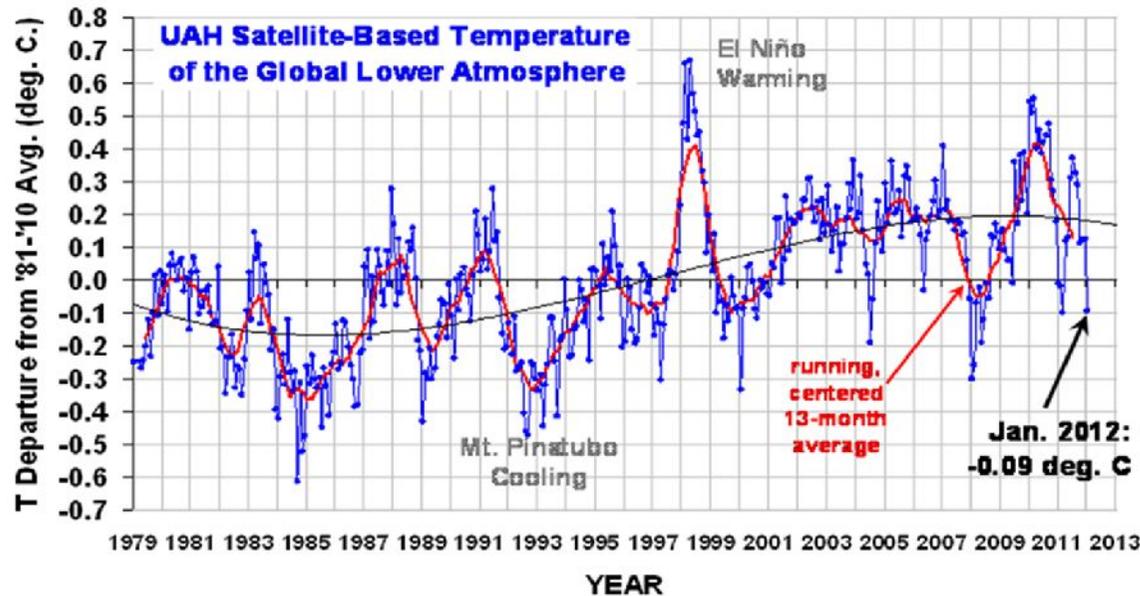
Friedrich-Karl Ewert
 FUSION 32, 2011, Nr. 3 p31

Oxford	0	-0.0076	0.0036	0.0188	-0.0136	0.0487	
Oslo	-0.0147	0.0105			-0.02	0.0783	
Minneapolis	0.400	-0.0625	0.0448		-1.360	0.0459	
New York		-0.0096	-0.002	0.0391	0.008	-0.148	
West Point	-0.0819	0.1053	-0.1125	0.0195	-0.0265	0.0138	
Jakutsk		0.014			-0.0299	0.0549	
St. Johns	0.089	-0.0131	-0.0018		-0.025		
Zürich		-0.015	0.0186		-0.0145	0.0452	
Vardo		0	0.0436		-0.0167	0.0326	
Beijing			0			0.08	
Stykkisholmur	-0.0389	0	0.0429		-0.019	0.0467	
Greenwich		0	0.05		0	0.0667	
Durham				0.0368	-0.028	0	0.0667
Jan Mayen		0.0143	-0.3	0.1167	0	-0.217	0.1833
San Francisco		-0.0079	0.0039		-0.00311	0.0633	
Gibraltar		-0.005		0	-0.03	0.045	
Luqa		0.0111		0	0.0181	0.1	0
Debrecen	0.02	-0.0148	0.0458	0	0.0135	0.028	
Nassau		0		-0.0208		0.0877	0
Nikolaevsk	0.0427	-0.0278	0.0111		0		
Buenos Aires		0		0.019		0.0789	
Hannover		-0.0276	0.053	-0.0288	-0.0046	0.0451	
Kapstadt	0.0341	-0.0152	0.0455	0	-0.0393	0	
Adelaide	-0.0379	0.0207	0		-0.0408	0	
Athen	-0.01	0	0.0583	0	-0.0292	0	0.0724
Sydney		-0.0014	0.0158		0.0088	0.0389	
Madrid	0	-0.0328	0.0294	0	-0.024	0.0952	0
Zagreb		-0.0255	0.037	0	-0.0172	0.0577	
Auckland		-0.0177	0.0166		-0.0095		
Wellington		-0.004	0.0338	-0.0046	0.0036		
Bukarest		-0.0438	0.0236		0	-0.0203	
Jakarta		0	0.0213		0		
Friedrichshafen		-0.0083	0.0198		-0.0012	0.052	

New Dehil	0.07	0	-0.03	0		
Chicago	-0.0184	0.0076	-0.0588	0.0252		
Montreal	0.0052	0.0388	-0.0135			
Kremsmünster	0.037	0		0.0591		
Tokyo	-0.0073	0.0293				-0
Alice Springs	-0.0141	0.0212	0.0631	0.0108		
Lissabon	0.0196	-0.025	0.0376	0		
Washington	0	0.0398	-0.0526	0.05	0	
Dublin	0.0159		0			
Darwin	-0.0058	0.0149		-0.00004		
Kagoshima	-0.0087	0.0044	0.0355			
Anrananarivo	0.034	-0.023	0.018			
Funafuti	-0.0222	0		0.0117		
Nuuk Godthap	0.0369	0	-0.1453	0.1124		
Werchojansk	0.0225	-0.022	0.0313	0.0019		
Flagstaff	-0.1023	0.0535	-0.0384	0.0442		
Reykjavik	0.0007	0.088	-0.0248	0.0654		
Santiago Chile	0	0.0455	-0.0316			
Caims	0.0009	-0.0047	-0.0121	0.0307		
Soul	0.0471	0		0.075		
Prince Rupert		0.0082	-0.0303	0.03		

At every point around the world, temperature increases, stays stagnant, decreases for rather lng periods of time, in an *oscillating* but **NOT exactly periodic way.**

Global temperature anomalies measured from satellites.

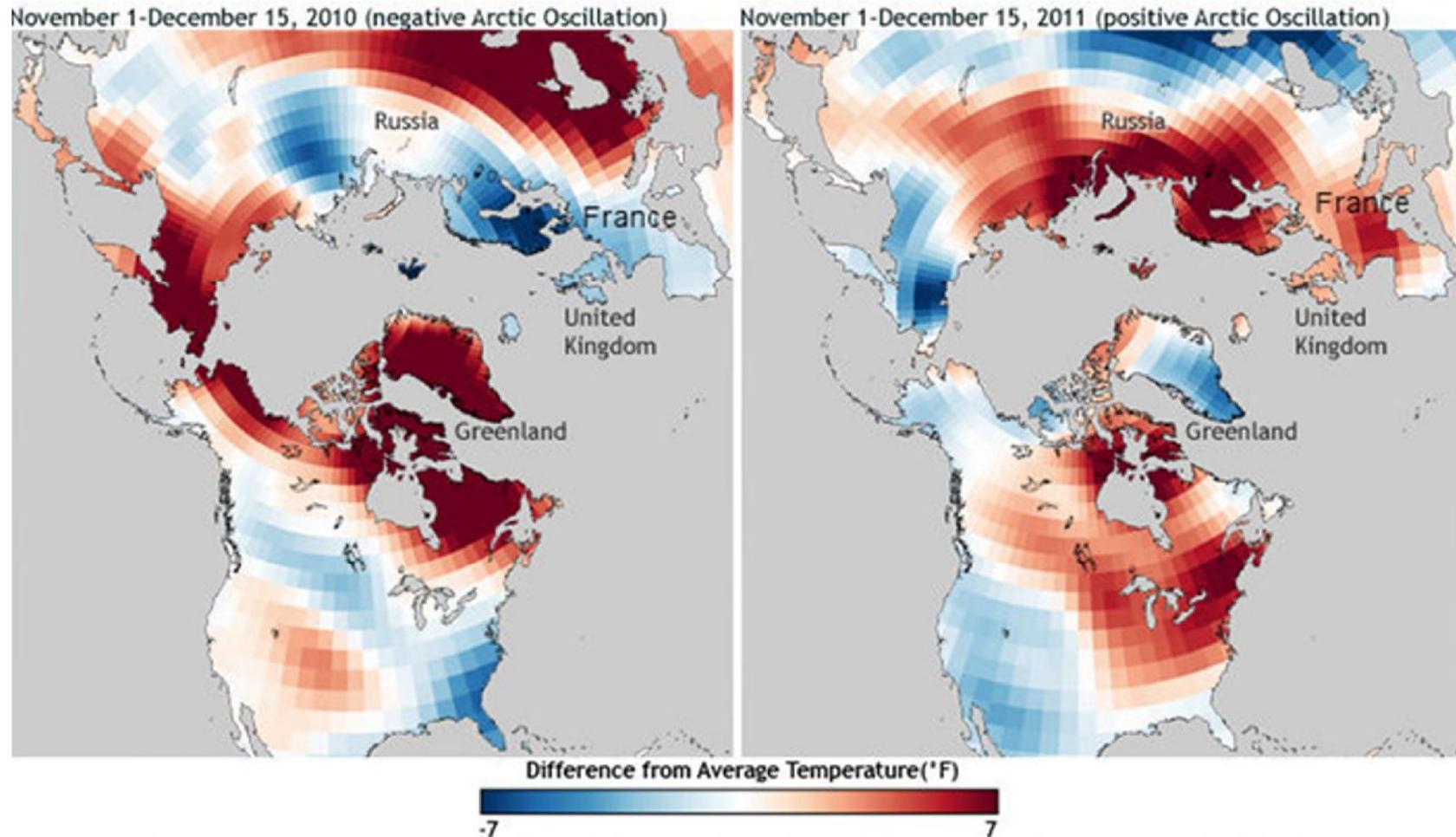


Temperature anomalies in the (very) low atmosphere as measured by satellites (over 33 years only) (*source* : figure by Spencer & Curry, redispached by Hans Labohm, *Dagelijkse Standaard*, 3 februari, 2012)

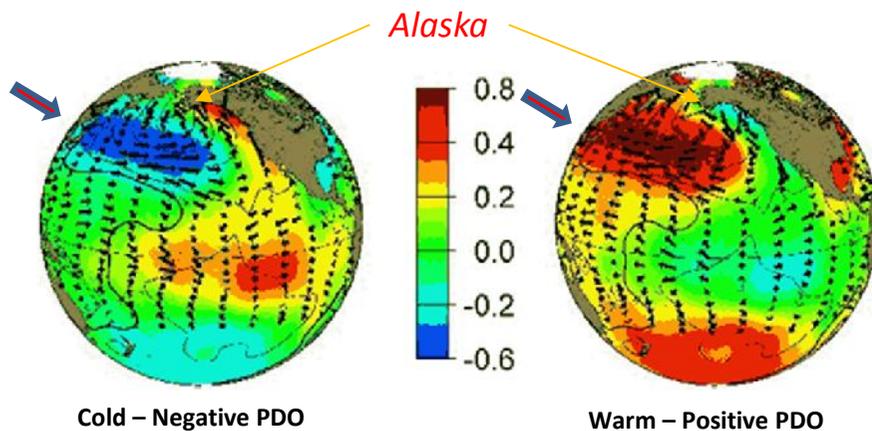
- **Evidence:** sensitive tool (natural « accidents » perfectly detected)
- **Evidence:** no (positive) trend observed
- **Evidence:** superposition of multi-periodic signals

More oscillations of temperature anomalies

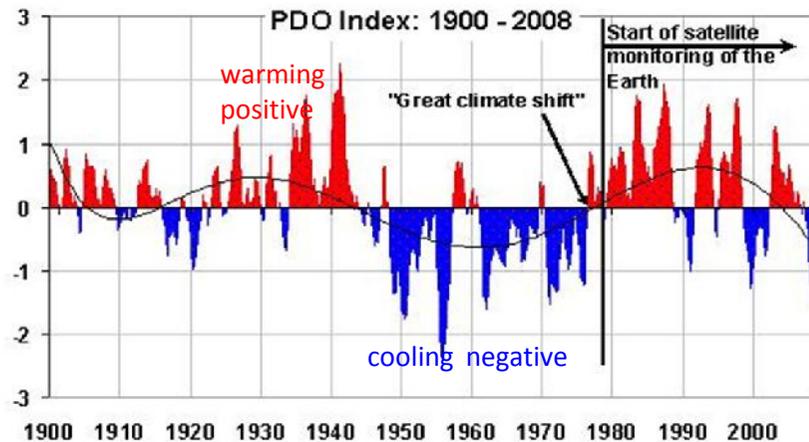
(Systematic inversion in almost all locations)



Comparison of temperature anomalies of the Northern hemisphere, over the same period during two successive years (source: NOAA Climate Service). **on the left side:** from 1st of November to 15th of December 2010. Under Negative Arctic oscillations conditions (AO-); **On the right side:** from 1st of November to 15th of December 2011. Under positive Arctic Oscillation conditions (AO+). *Note: anomalies given in Fahrenheit temperature scale. $^{\circ}\text{C} = 5/9 * (^{\circ}\text{F} - 32)$. For temperature anomalies, the conversion factor is 5/9 (anomalies are temperature differences: actual temperature – local average over 30 years[1960-1990])*



Source of diagram: jisao.washington.edu



Source of diagram: Spencer (2012)

The **driving mechanism** of the PDO COULD be of the astronomical-physical type, involving *in-line gravitational interaction of Jupiter, Saturn and Sun affecting Pacific tidal activity* (Scafetta, 2010).

Pacific Decadal Oscillation

PDO measures the difference in atmospheric pressure between Japan and Alaska. It is said to affect strongly US weather conditions

Mainly in the **North Pacific** two different oceanic and atmospheric circulation patterns alternate every 20-30 yrs with a cyclicity of 40-60 yrs, causing changes in areas of warm and cold surface waters.

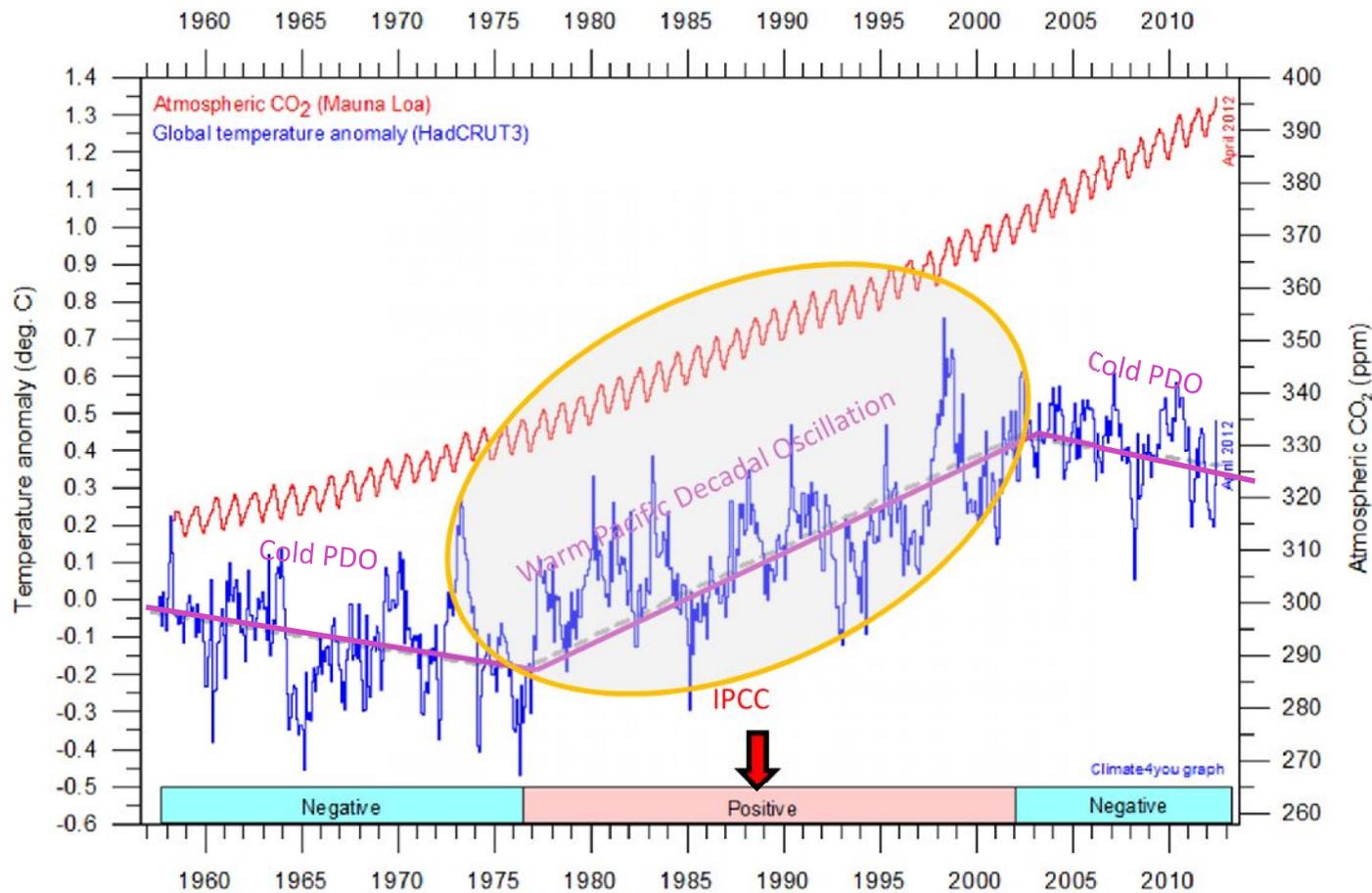
A clear PDO/temperature relationship does exist.

Modeling and satellite data show that the cloud cover of oceans decreases slightly during positive PDO phases but increases slightly during negative PDO phases. This affects the Earth's Albedo and, by radiative forcing, the climate (Spencer, 2008).

Recently the PDO entered a new negative phase, thus contributing to the present decline of global average temperatures.

GCM models neglect PDO effects

Since 1958 global surface air temperature and atmospheric CO₂ concentrations correlate only partly while there is a striking correlation between the Pacific Decadal Oscillation and temperature.

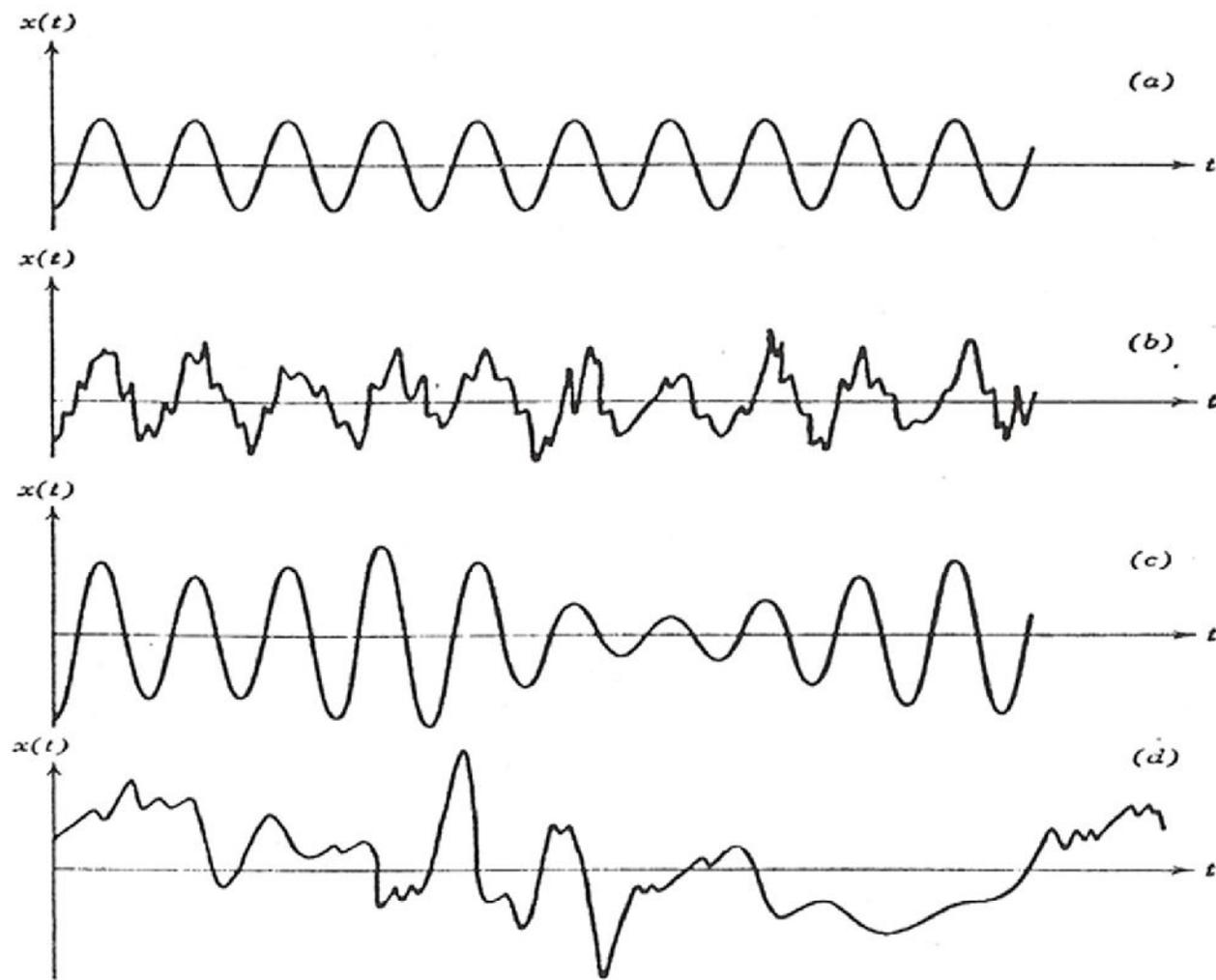


Source: Climate4you Greenhouse Gases

Similar to the HadCrut3 temperature curve, the NCDC, GISS, RSS MSU and UAH MSU curves show the same **ABSENCE** of temperature relationship to atmospheric CO₂ concentrations, over the last 50 years

(Note: red arrows shows the 1988 start-up of IPCC and the Anthropogenic Global Warming Scare, based EXCLUSIVELY on the 1978-2002 time window)

SOME COMMON SIGNAL PATTERNS



Four special time histories. (a) Sine wave. (b) Sine wave plus random noise. (c) Narrow-band random noise. (d) Wide-band random noise.

Two kinds of noises

Random Noise

- Mean value is zero
- Gaussian distribution (bell shaped)
 - Completely defined by mean value and variance
 - Statistical parametric methods are applicable
 - Error on mean value diminishes as $\sqrt{1/(N-1)}$

Chaotic (Dynamical) Noise

- Deterministic non-linear equations
- **Extremely** sensitive to initial conditions and value of parameters
 - => **Practically non-predictible on the medium or long term.**
- Amplitude distribution is **NOT gaussian**. Points fluctuate in the vicinity of several « **strange attractors** » around which they fluctuate in an approximative periodic way.
 - => **Mean value is meaningless**, as the probability that points are in its vicinity is very low.
 - => **The mean value is NOT longer representative of the signal**

NON LINEAR ANALYSIS OF SIGNALS

Non linear analysis of signals

What to measure?

- Amplitude distribution
- Time recurrence (or its inverse the frequency)
- Predictibility

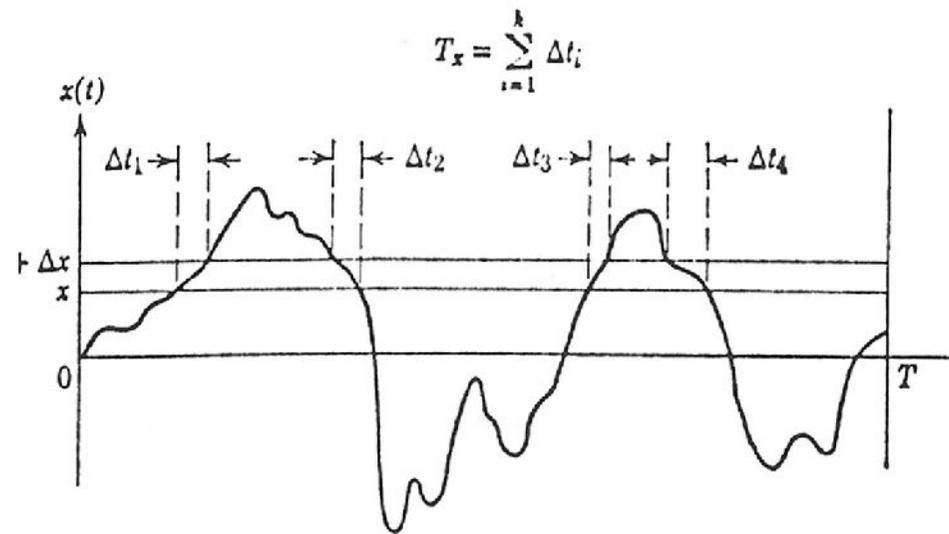
What to detect?

- Trends (shifts)
- Periodicities
- Chaotic signature
- Differentiating chaotic from random noise

Which toolbox?

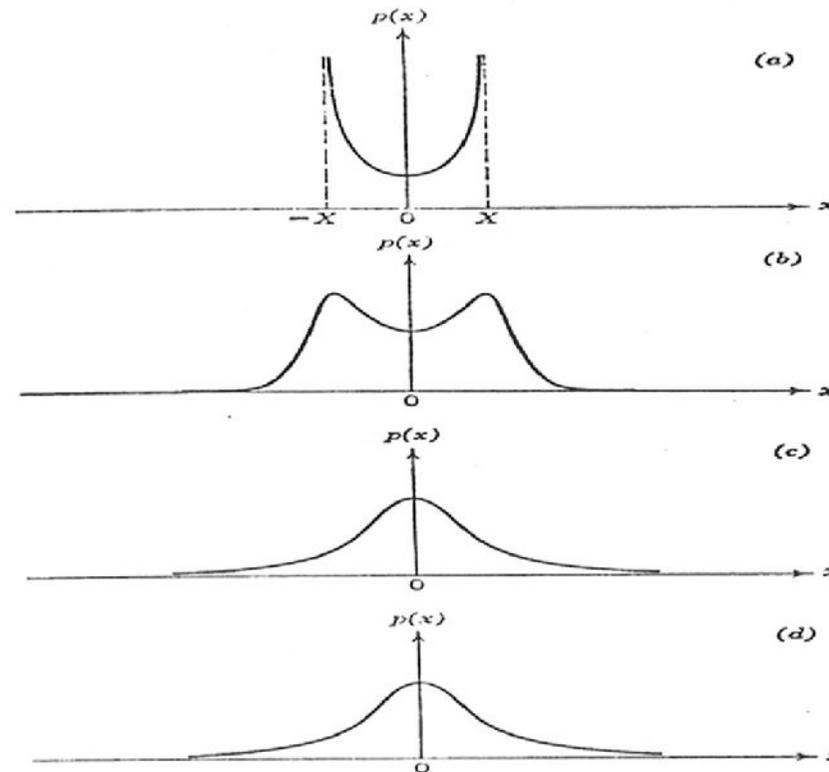
- Amplitude analysis
- Autocorrelation
- Fourier analysis
- Power spectrum
- Phase diagrams
- Recurrences + toolbox
- (non parametric predictibility of time series)
- Wavelets

Amplitude Analysis



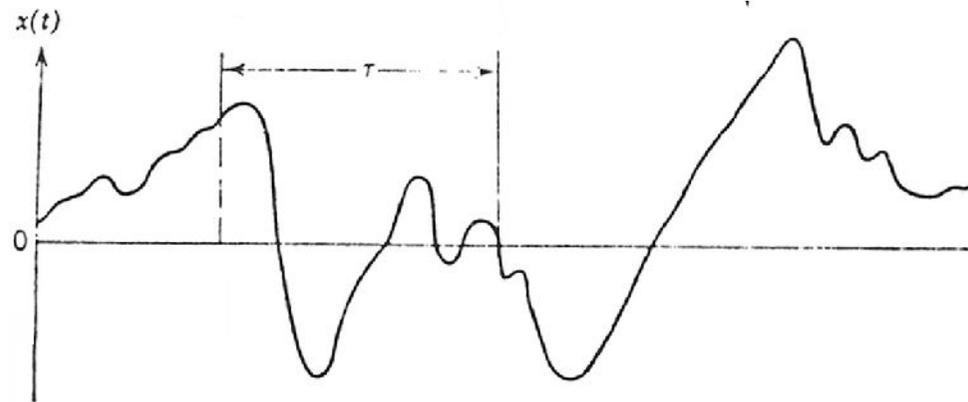
Probability measurement.

Examples of Amplitude Distributions



Probability density function plots. (a) Sine wave. (b) Sine wave plus random noise. (c) Narrow-band random noise. (d) Wide-band random noise.

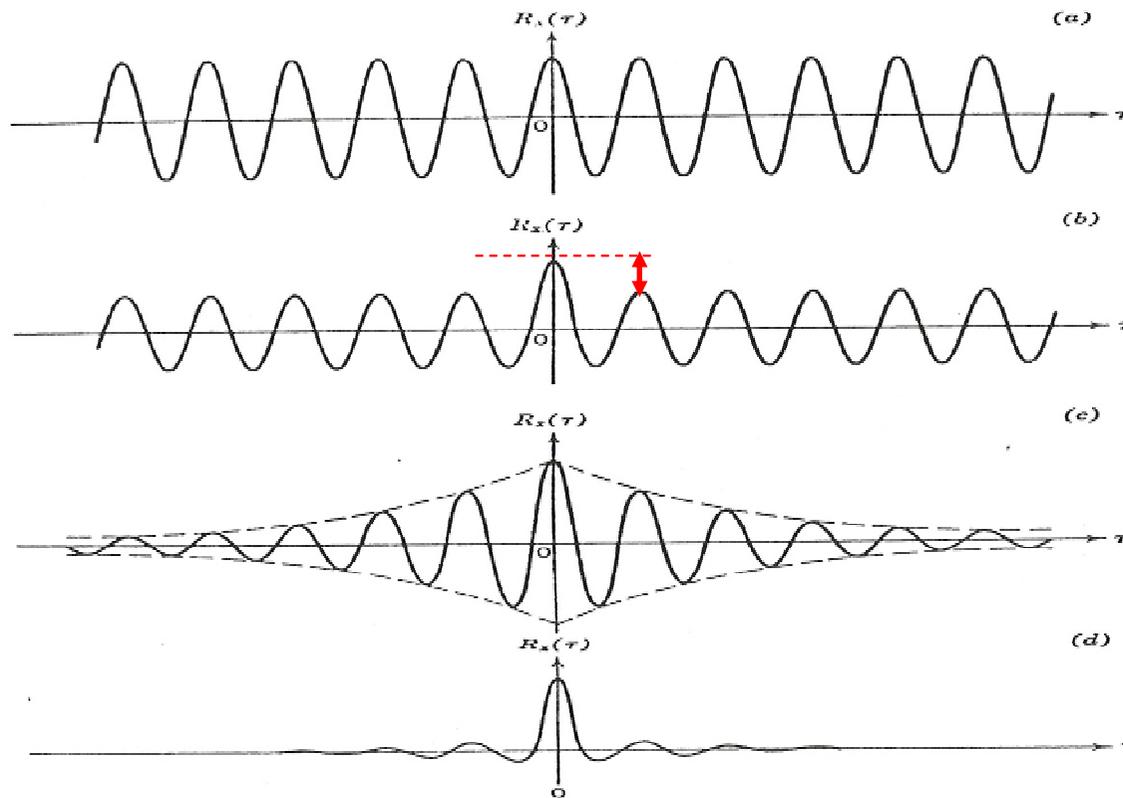
Time auto-correlation



$$\rho(\tau) \stackrel{\text{def}}{=} \frac{1}{n} \sum_{i=1}^n X_i X_{i+\tau}$$

Autocorrelation measurement.

Examples of autocorrelation functions



Autocorrelation function plots (autocorrelograms). (a) Sine wave. (b) Sine wave plus random noise. (c) Narrow-band random noise. (d) Wide-band random noise.

Power Spectrum

- Fourier Transform of the auto-correlation function

$$P(f) \stackrel{\text{def}}{=} \int_{-\infty}^{\infty} \rho(\tau) e^{-i2\pi f\tau} d\tau$$

- **IMPORTANT: Shannon sampling theorem**

- Max frequency detectable = $\frac{1}{2}$ sampling frequency (\Leftrightarrow smallest period detectable = 2 times time interval between samples)
- Information lost when averaging from hour to day to month to quarter to year to decade to century to millenium, etc.

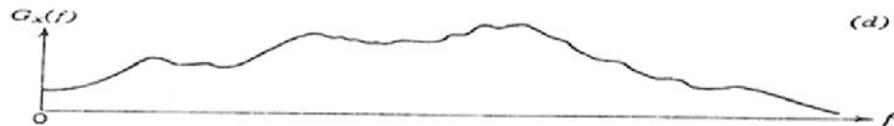
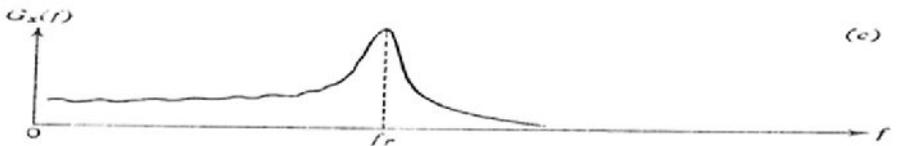
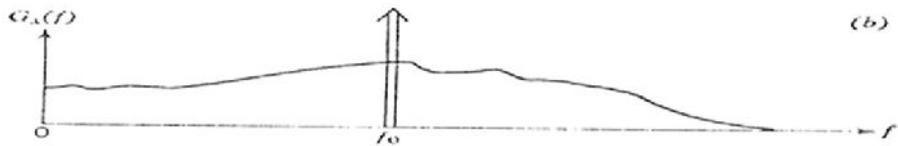
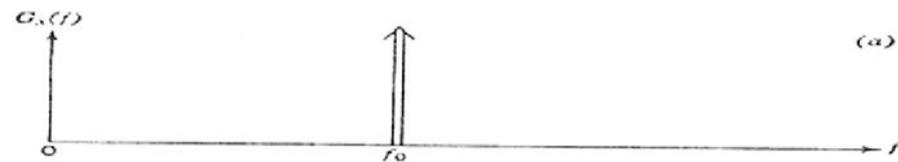
- **IMPORTANT: end effects:** maximum period detectable $\sim 1/3$ of time window of the time series

- “Reconstruction” is possible by Inverse Fourier Transform

$$X(t) = a_0 + \sum_{i=1}^{\infty} (a_i \cos(\omega_i + \varphi_i)t + b_i \sin(\omega_i + \varphi_i)t)$$

Provides a physical meaning: the amplitude, frequencies and phases of a set of sinusoids (and cosinusoids) giving the best fit to the time series (or signal)

Examples of Power Spectra



Power spectral density plots (power spectra). (a) Sine wave. (b) Sine wave plus random noise. (c) Narrow-band random noise. (d) Wide-band random noise.

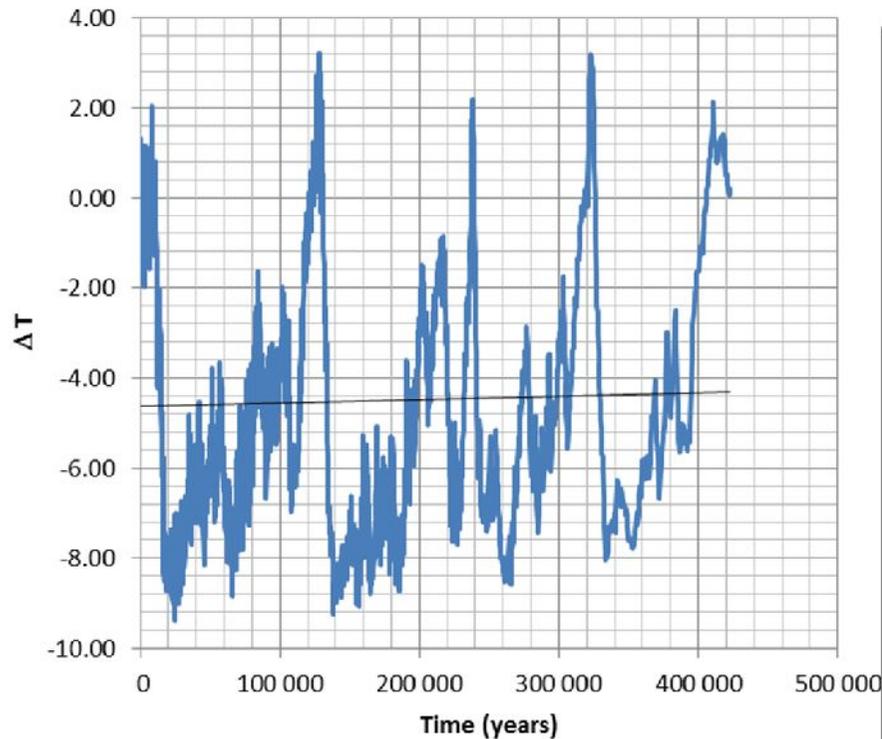
Vostök (from isotopic analysis of ice rods & included bubbles)

Spatial Averaged temperatures 30-60°N

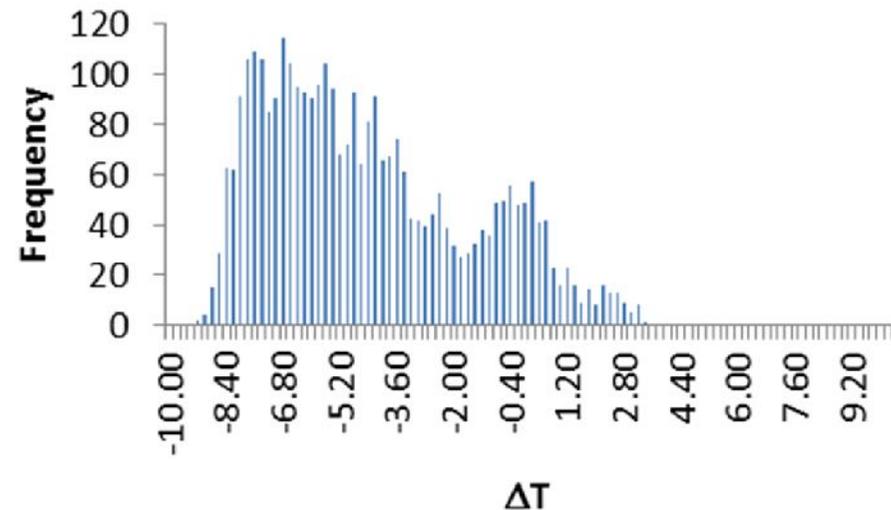
Local temperatures Uccle Meteo station (Brussels, Belgium)

APPLICATION TO LAND TEMPERATURE MEASUREMENTS.

Time Series of Vostok's Temperatures

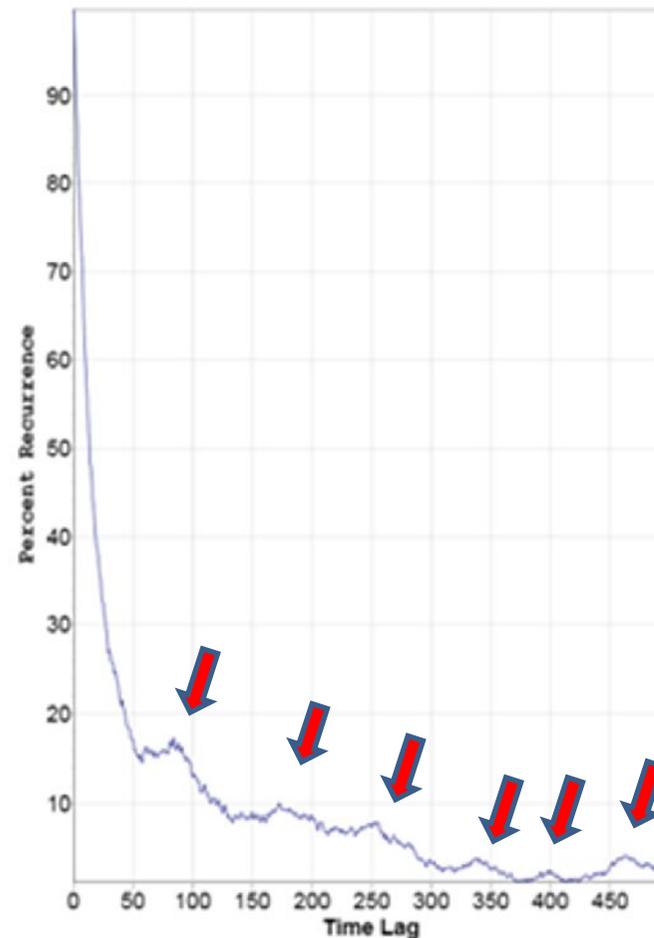


ΔT Histogram (Vostok Data => -400 000 years)



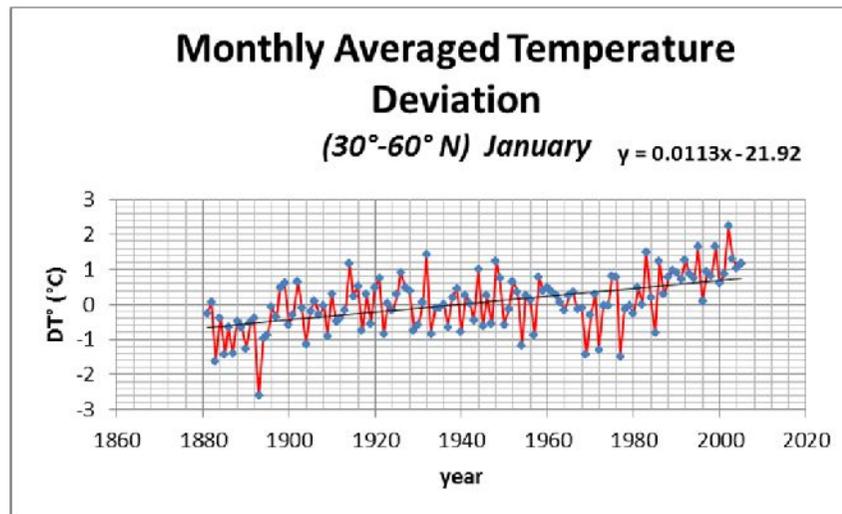
Amplitude analysis of temperature anomalies estimated from ice rods at Vostok. The amplitude distribution is *NOT gaussian but bimodal*. The main mode corresponds to glaciation conditions (6 to 8°C lower than presently (with a mode at -6.8°C). A secondary peak corresponds to a « temperate » climate, fluctuating around the a-present temperatures (with a mode 0.4°R lower) as the one prevailing presently. The temperature never exceeded over 400 000 years the present temperature by more than 3.2°C.

Autocorrelation of Vostök data. The horizontal axis refers to the order of the sample in the time series? Unfortunately, the time interval between successive data is not totally constant, but the scale is approximately expressed as Kyears. The periodicities detected (local maxima in the curve) are thus only approximate. Points are expressed as anomalies towards the temperature averaged over the 20th century. The important peak at origin corresponds to the sum of the square of the mean value (corresponding to a bias in the data) and the variance of the signal. Periodicities have been linked to the Planets' ***Milankovitch cycles*** (Berger et al, 1988).



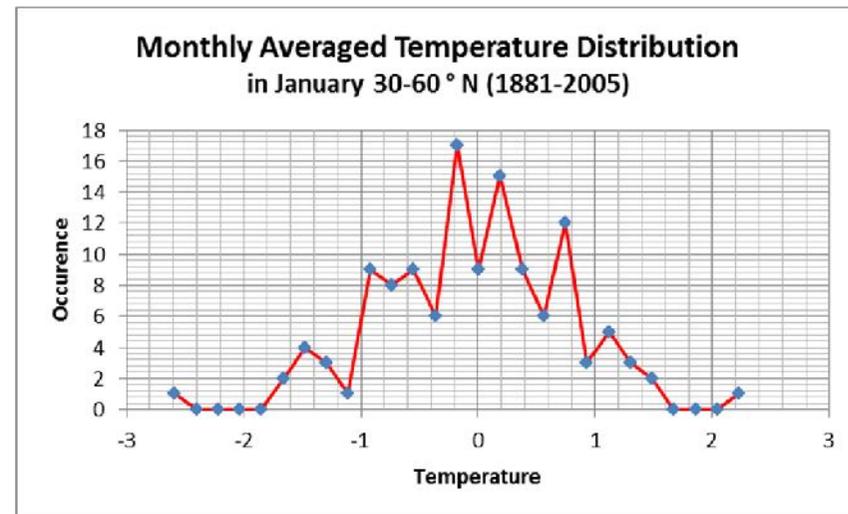
Analysis of spatially averaged temperatures

Time series



125 Data points

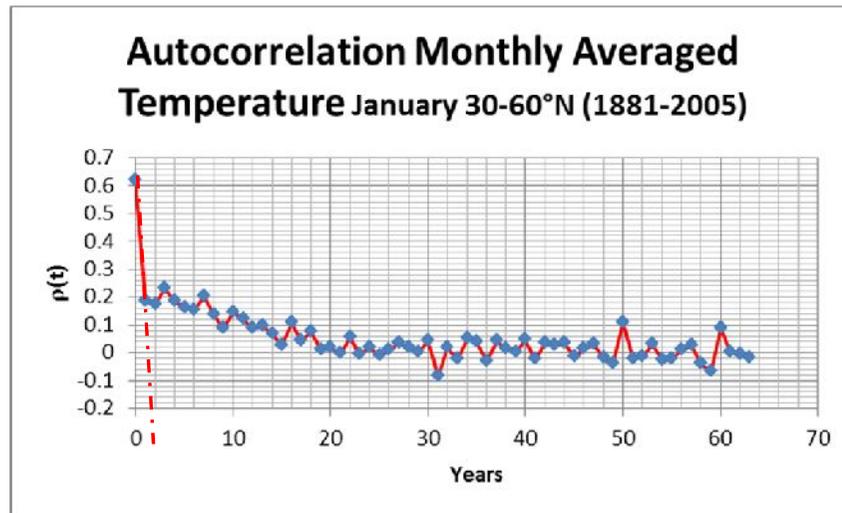
Amplitude distribution



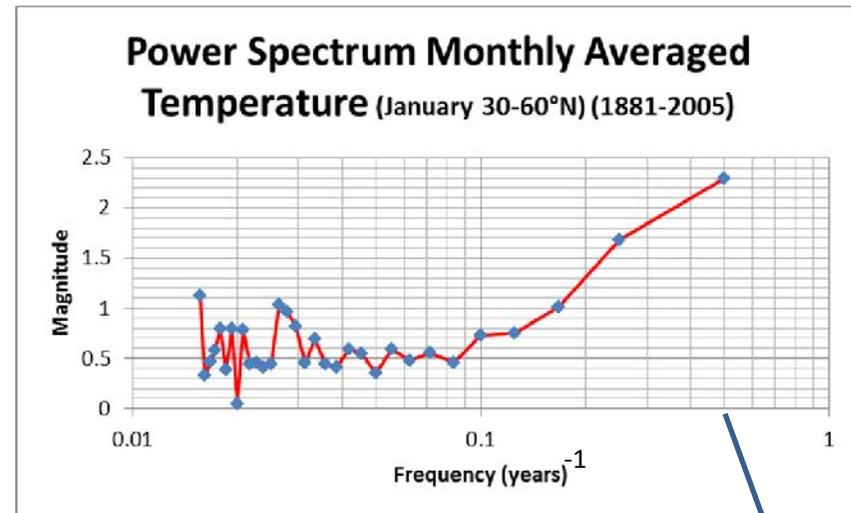
The amplitude distribution is *not gaussian* (as can be tested with a χ square test). Strictly speaking, *usual statistics (i.e. regression lines)* may not be applied.

Analysis of Temperature

Time autocorrelation



Power spectrum

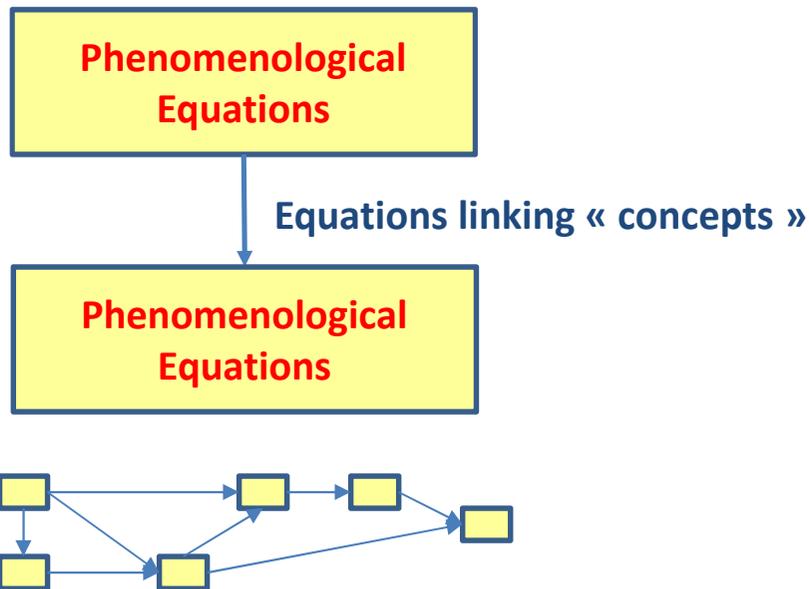


Shannon
Frequency :
 2 years^{-1}

TEMPERATURE RECONSTRUCTIONS USING FOURIER ANALYSIS

Two different approaches

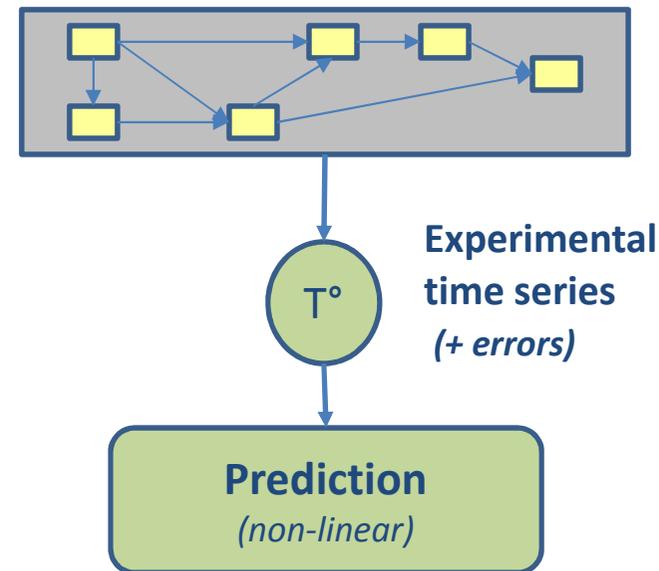
IPCC – Descriptive model



*If the algorithm contains an equation stating that temperature increases when anthropogenic carbon emissions increase, the results will show such a pattern. **THIS IS NOT A PROOF...***

*What if one concept has been forgotten?
What if one of the links has been forgotten?
What if one of the links has been wrongly formulated?*

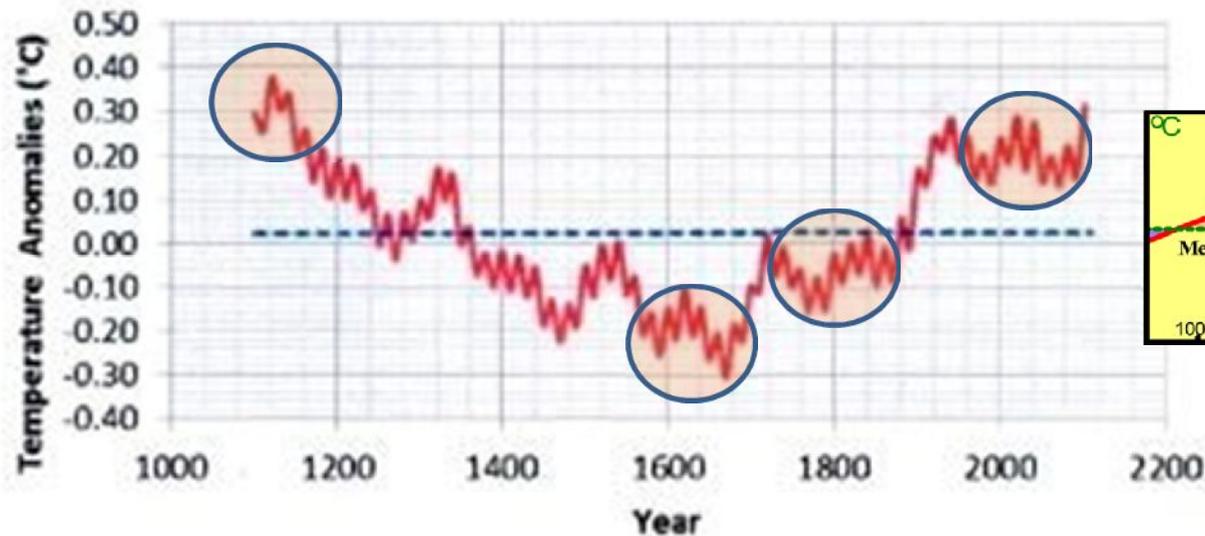
Black box – predictive model



*Exclusively based on experimental data (unfortunately non perfect)
Requires limited computer facilities => easier to assess*

*Better adjustment than descriptive models?
Predictability horizon (& error margin)?*

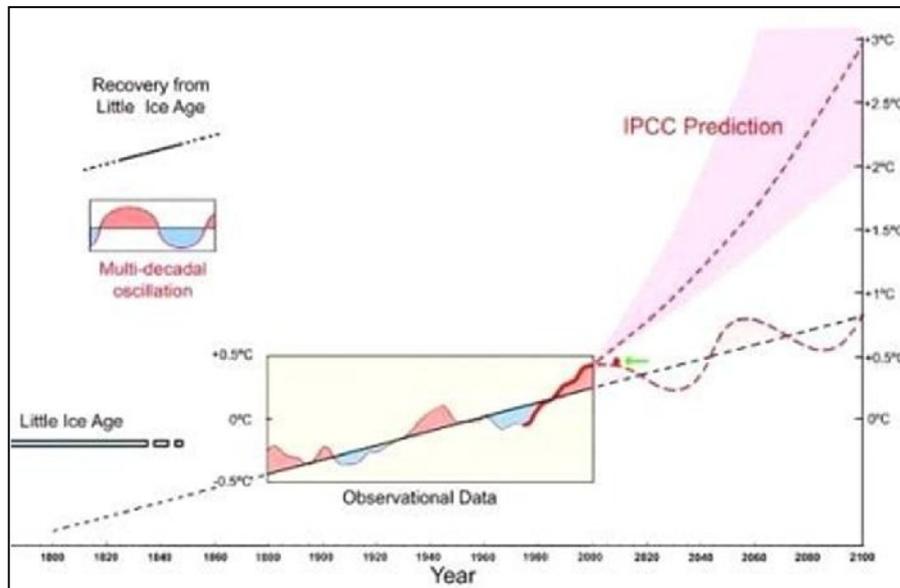
Simulation of Temperature Anomalies



	Amplitude	Period (in N steps)	Pulsation	Frequency	Phase (degrees)
Curve A	6	2	3.142	0.500	50
Curve B	5	10	0.628	0.100	0
Curve C	6	20	0.314	0.050	20
Curve D	3	50	0.126	0.020	140
Curve E	20	99	0.063	0.010	90
Random	4				

Calibration Ox		Calibration Oy	
Time scale		Temperature (Anomalies)	
	year		
Initial date	1100	°C/unit	0.05
increment	10		
N of steps	100		
Final date	2100		

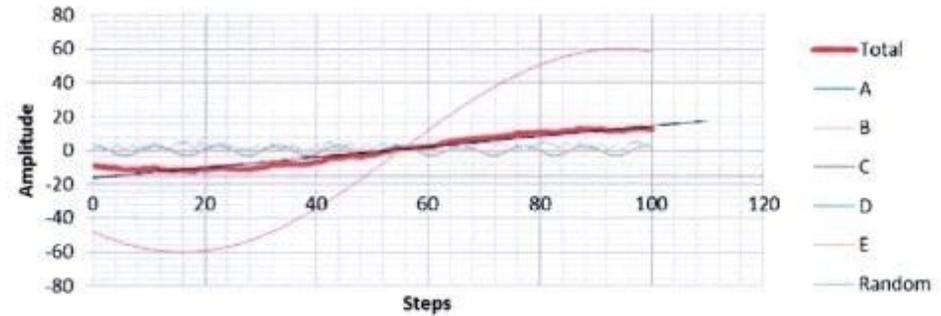
- A simple approximation by Fourier series (sum of sinusoids)
- A « black box » approach. Predicting does not require modeling. (i.e. best model for tides prediction is a black box model....and this remains the best predictive tool for more than a century....)



The figure shows that the **linear trend** between 1880 and 2000 is a **continuation of recovery from the LIA**. It shows also the predicted temperature rise by the IPCC after 2000. Another possibility is also shown, in which the recovery from the LIA would continue to 2100, together with the **superposed multi-decadal oscillation**. This possible progress beyond the peak of an oscillation could explain the halting of the warming after 2000. The observed temperature in 2008 is shown by a red dot with a green arrow. (source : Akasofu, 2009)

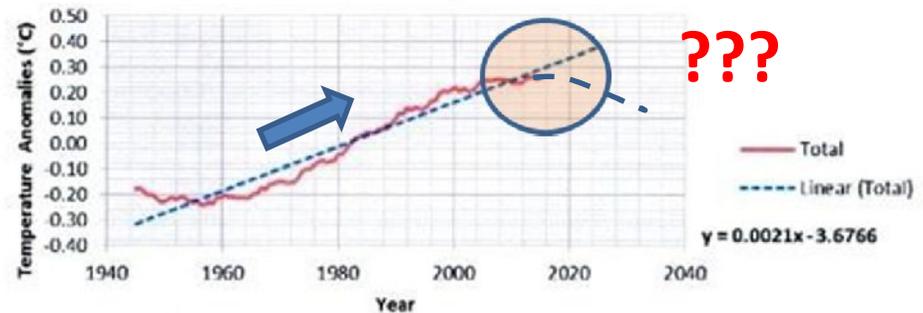
But: The « linear trend » is best replaced by a centennial wave (+ some noise)

Sum of Sinusoids+ Random Noise



Superposition of two sinusoids & random noise (*sinusoid A: amplitude: 3; period: 11; initial phase: 86°; sinusoid B: amplitude: 60; period: 156; initial phase: 233°; white random noise amplitude: 5*)

Simulation of Temperature Anomalies



Same figure recalibrated (*Ox: initial year : 1945 ; step: 0.7; number of steps: 100 ; final year :2010 . Axe Oy : 0.02 °C/unit*)

The climate system is extremely complex

Synchronisation mechanisms

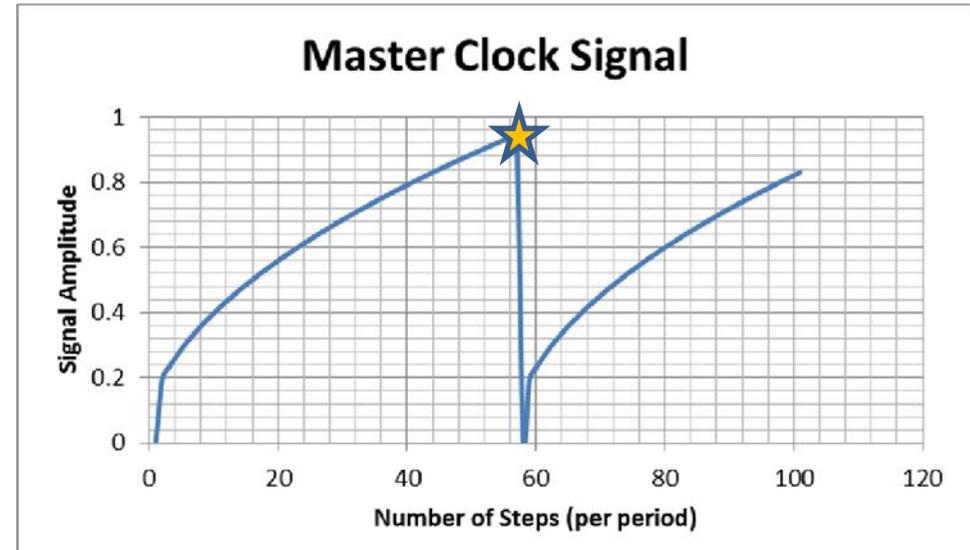
Where is the master clock?

SYNCHRONISATION IN COMPLEX SYSTEMS

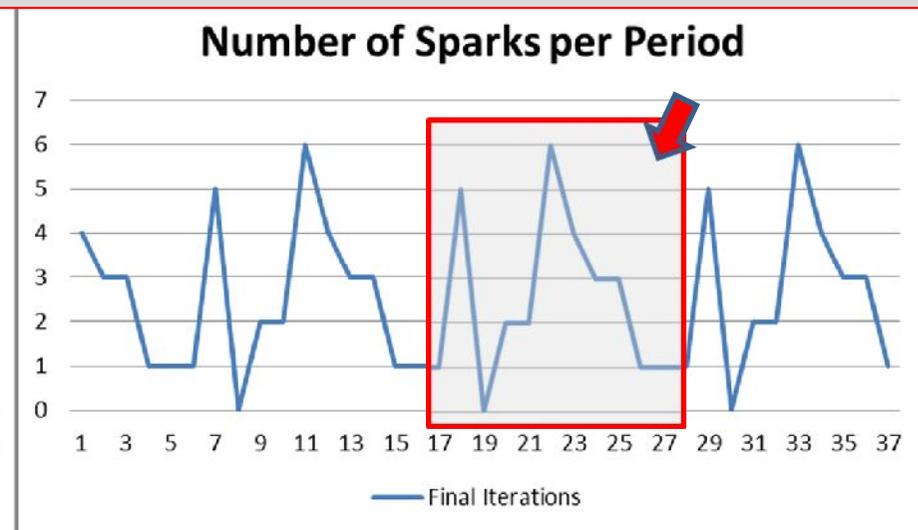
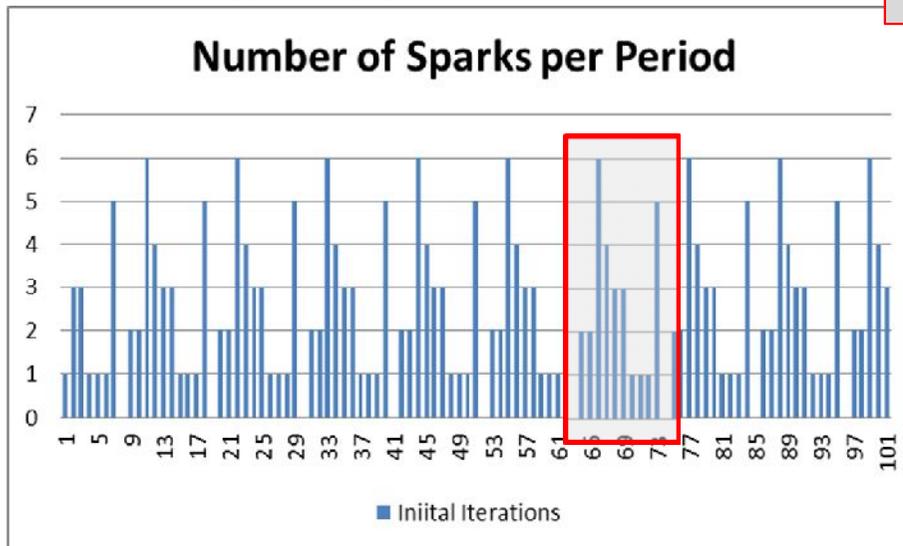
Synchronisation of complex systems

Legion synchronisation

- A « *master clock* »
 - Corresponding to an « *accumulator* » (↔ electrical capacity)
 - (adjustable) load curve (stepwise)
 - at (adjustable) threshold level: a « flash » followed by instantaneous discharge
 - Provides initial « flash »
- N « *slave* » oscillators
 - Receive a load « quantum » when any other oscillator « flashes »
 - « Flash » & Send a load « quantum » to every other oscillator when they reach their own threshold level



Rather quickly the phases of the oscillators become locked. A characteristic pattern is repeated.



Where is the master clock ?

- Solar or planet conjunction cycles?
- Complex systems also exhibit **synchronisations**
 - No strict causality link but discontinuous mutual influence
 - Each concept send « flashes » to the other concepts when it reaches a certain threshold level (Legion effect)
 - Does Exist in nature
 - Pendula synchronisation in a same room
 - Crickets; light worms
 - Josephson diodes, etc.
- **CAUTION: Approximative Synchronism is NOT Causality but Intermittent mutual influence through (eventually complex & indirect) feedbacks**

Centennial gravity interactions

Decandole (2003) computations over the 1800-2032 period

Number of conjunctions	Concerned planets	Cycle length (years)
14	Jupiter & Neptune	178.95
13	Jupiter & Uranus	179.55
9	Jupiter & Saturne	178.73
5	Saturne & Neptune	179.35
4	Saturne & Uranus	181.14
1	Uranus & Neptune	171.44

There is clearly a **179 years periodicity**,

Or more exactly several 179 years cycles, that are phase shifted

Such cycles do interfere with ***solar activity*** (by changing the ***angular momentum*** of the sun towards the gravity centre of the solar system, generating solar « ***hot spots*** » ***and eruptions***, modifying ***the magnetic field of the Sun and the Earth***.

Also the ***rotation axis of the Earth and its trajectory*** could be affected

Some well known solar cycles

« Classical » cycles

Duration (years)	Name	Latest cold period	Next cold period
11	Schwabe		
22	Hale		
24-29			
60			
87-90	Gleissberg	1996	2030
180	Harmonic 2 of Gleissberg cycle?		
208-210	Suess	1898	2210
232		1876	2038
~ 1 000			
2 300	Halstadt		
6 000	(Xapsos & Burke)		

Milankovitch cycles (1922)

- 40 Kyears
- 100
- Etc.

Cycles Identified usng C¹⁴ (Damon & Sornett ,1991)

- 105 years
- 131
- 232
- 385
- 504
- 805
- 1500
- 2241

CHAOTIC SYSTEMS

A Simple Chaotic Function: *The Logistic (Quadratic) Equation*

For this purpose, one best looks at one of the simplest dynamical systems: the one where a single positive and negative feedback try to balance each other (*logistic equation*, also known as quadratic or *Verhulst equation*):

$$X_{t+1} = \alpha X_t (1 - X_t) \quad [1]$$

Where α is a parameter

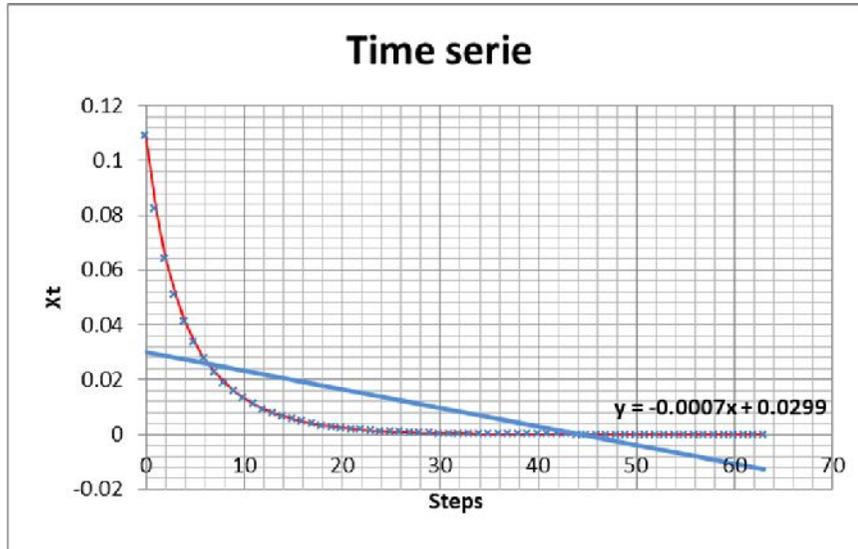
- If $0 < \alpha < 4$, the value of X_t remains between 0 and 1; the function presents a maximum for $X = \frac{\alpha}{4}$

For an initial value $X_0 = 0.6876$, and increasing values of α , X_t :

- goes asymptotically to zero (extinction) for $0 \leq \alpha \leq 1$
- goes asymptotically to an asymptotic value $L = 1 - \frac{1}{\alpha}$ for $1 < \alpha \leq 2$
- goes to the same equilibrium value, but from both side (damped oscillations) for $2 < \alpha \leq 3$
- quits progressively the equilibrium value and starts to oscillate between two values, for $\alpha = 3.2$

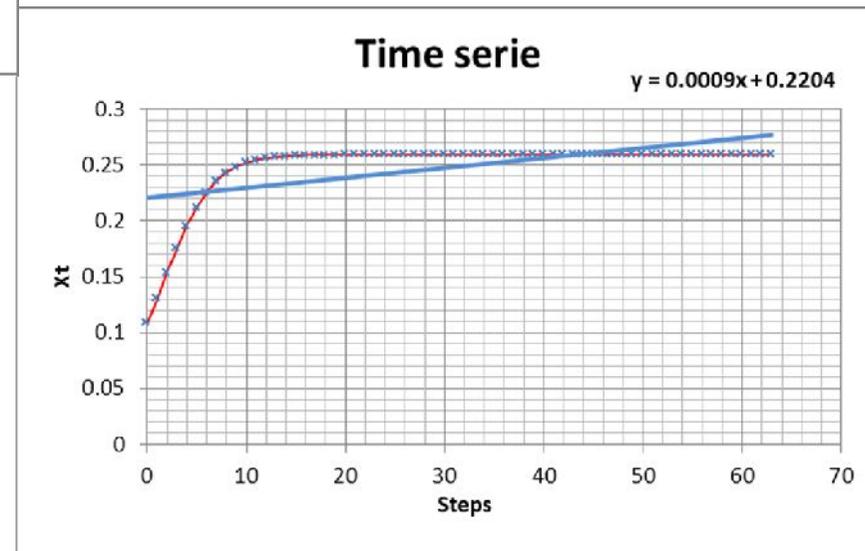
Logistic equation

Extinction or asymptotic saturation



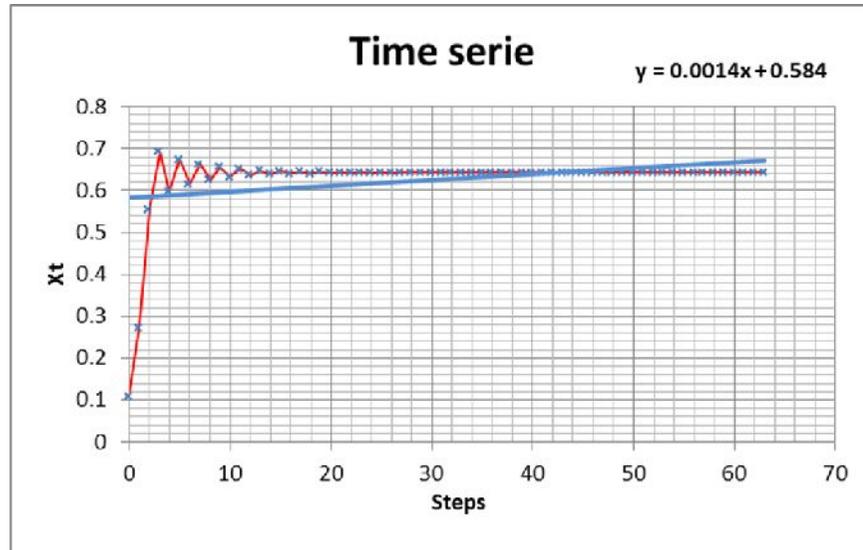
$$X_0 = 0.109$$
$$\alpha = 0.85$$

$$X_0 = 0.109$$
$$\alpha = 1.35$$



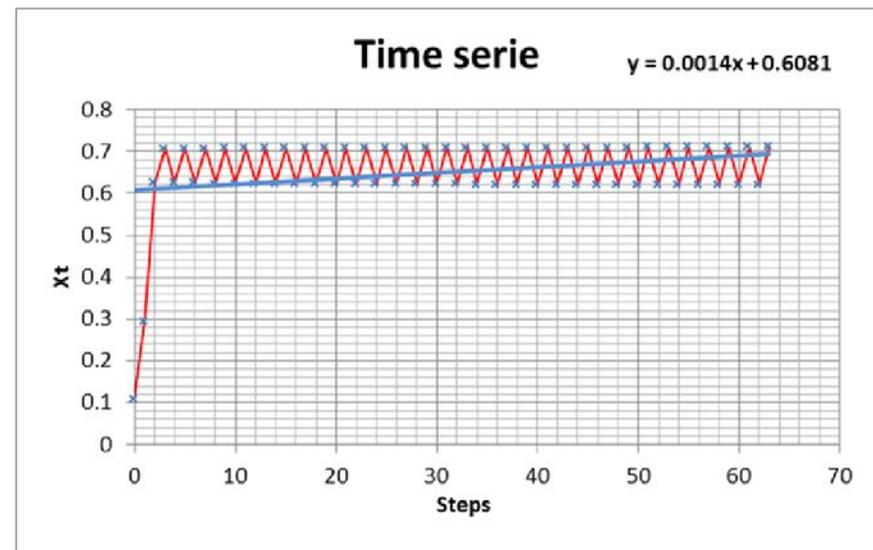
Logistic equation

Oscillating behaviour (damped or stabilized)



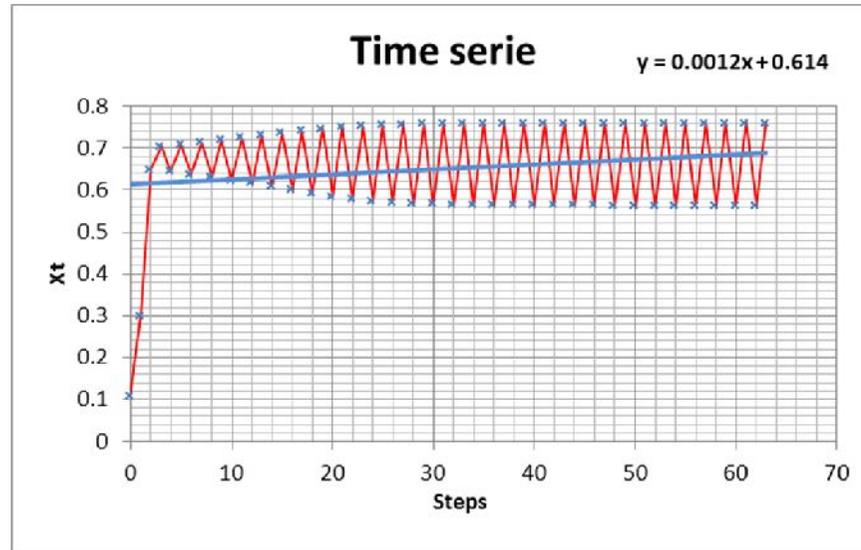
$$X_0 = 0.109$$
$$\alpha = 2.8$$

$$X_0 = 0.109$$
$$\alpha = 3.01886$$



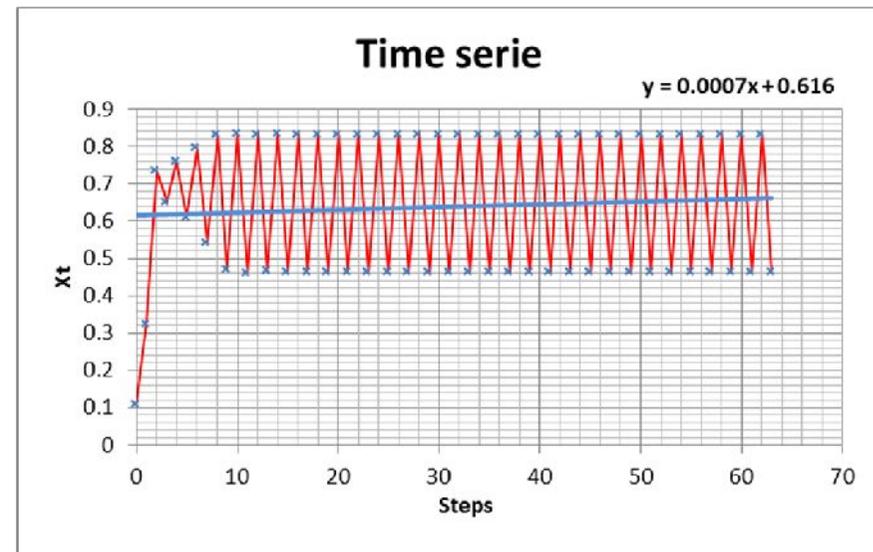
Logistic equation

Oscillating behaviour (divergent)



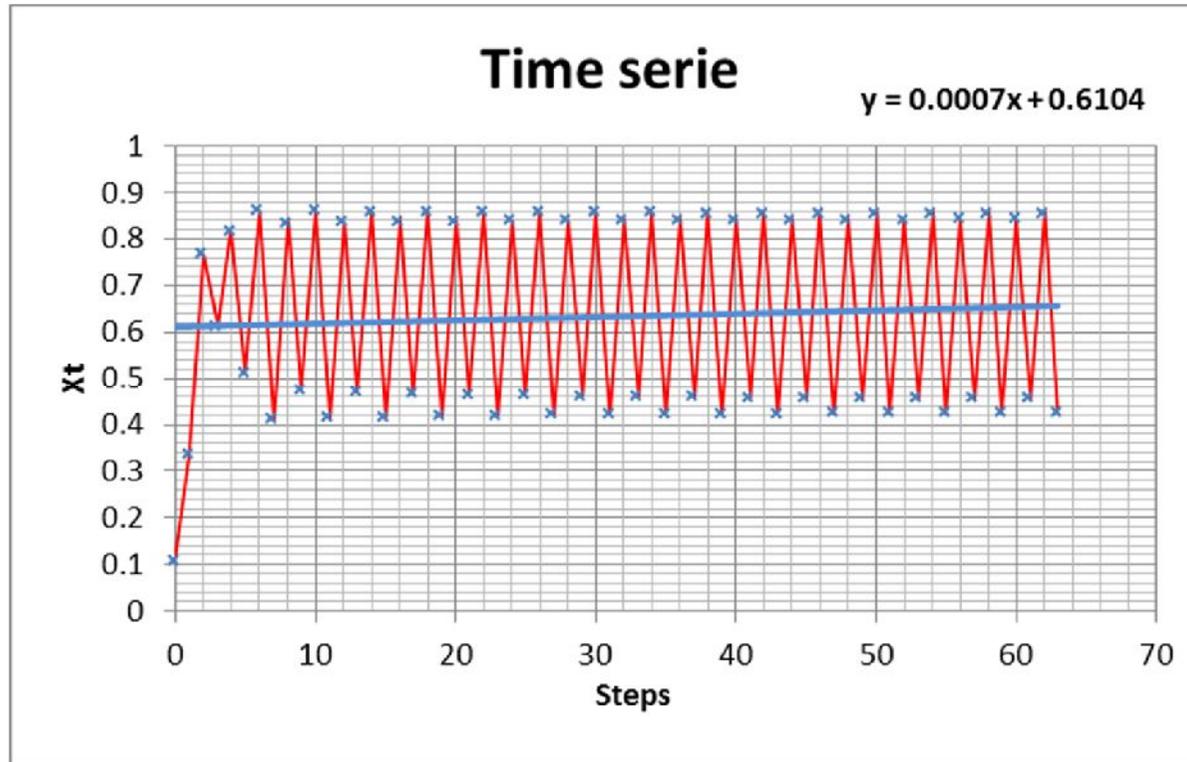
$$X_0 = 0.109$$
$$\alpha = 3.09$$

$$X_0 = 0.109$$
$$\alpha = 3.35$$



Logistic equation

slightly chaotic signal



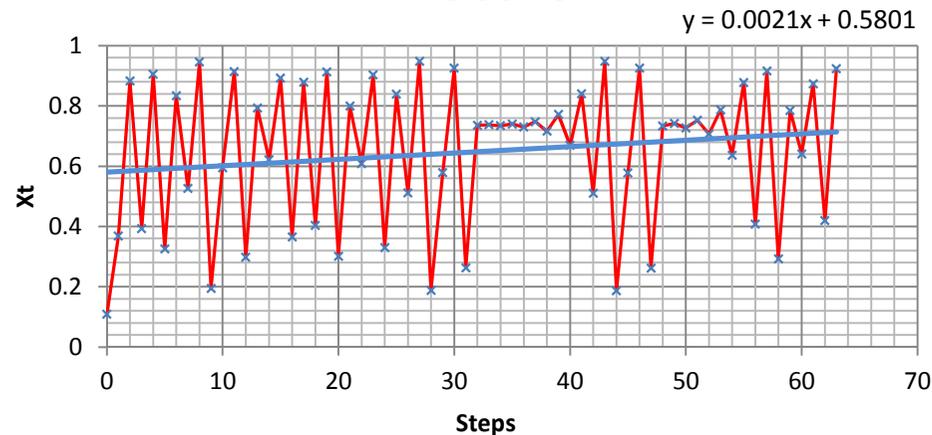
$$X_0 = 0.6, \alpha = 3.45$$

The periodic signal has split in two components (*bifurcation*)

Logistic equation

Evolution towards a more chaotic state

Time serie



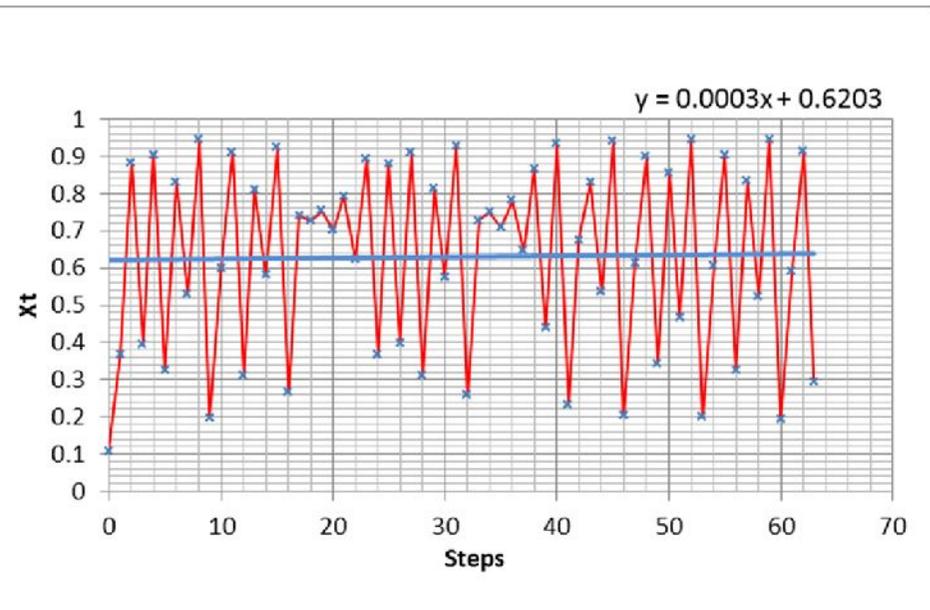
Logistic equation ($X_0 = 0.109$; $a = 3.79304$) showing a slight positive trend versus time.

Logistic equation ($X_0 = 0.109$; $a = 3.79354$) showing almost no trend versus time

Whatch out:

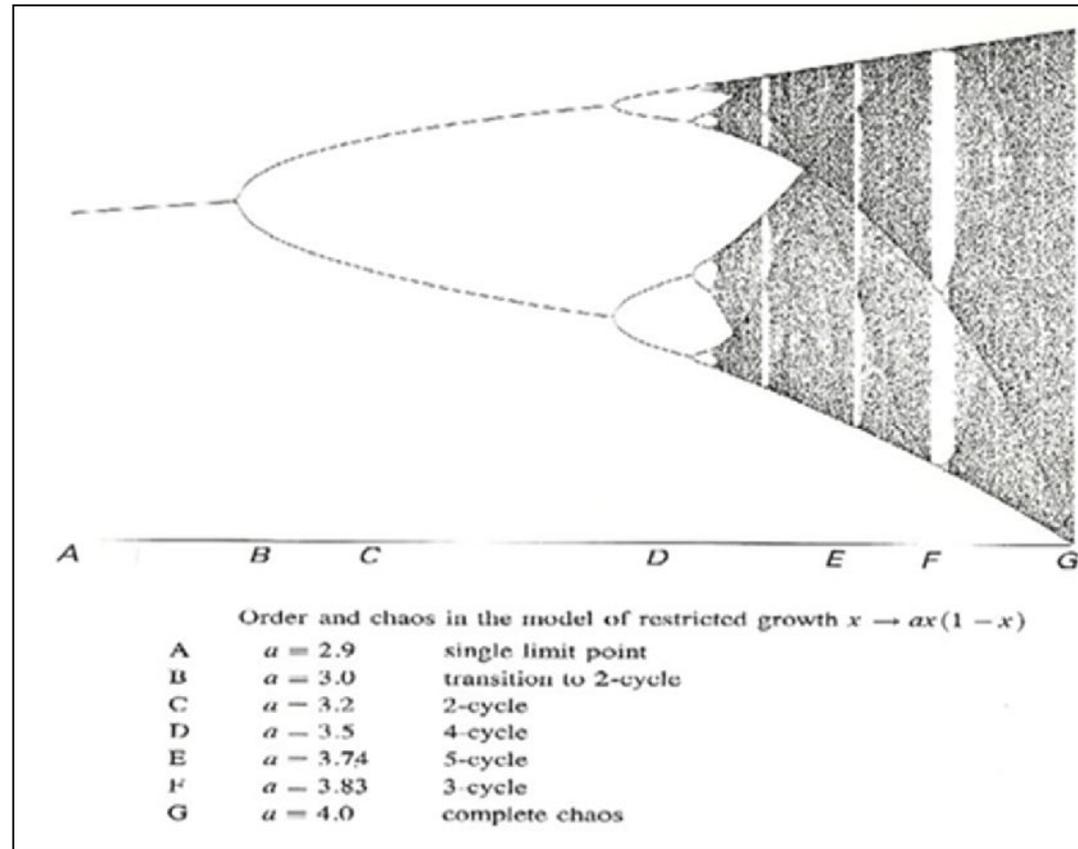
- *Tiny difference in value of the parameters*
- *Periods of relative stability*

**Purely deterministic equation
but Predictability from time series?
Meaning of the regression line?**



Sensitivity to parametre α

- When the parameter α is increased, the signal becomes oscillating,
- then the frequencies split in more and more (sub)harmonics, at some BIFURCATION points
- Chaos corresponds to a very large number of harmonics
- Some stable windows exist between very chaotic situations.



It is possible to detect the “signature” of a system evolving progressively towards a chaotic state by identifying the occurrence of bifurcation points

Phase Plan

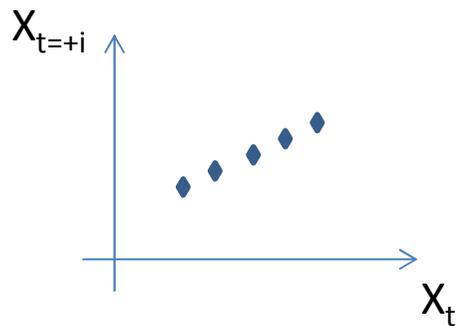
- Based on *Tokens* Theorem:
 - Phase plan (Comweb graph) can be constructed from time series

$$X_{t+i} = f(X_t)$$

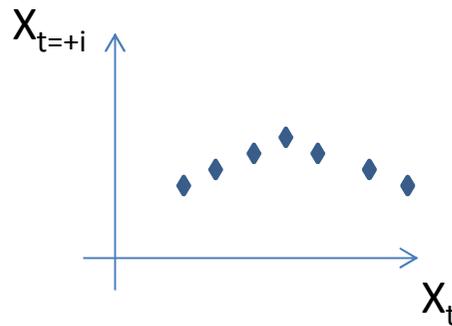
- **i = embedding dimension:** a way to analyse the predictability of the signal
- Can be extrapolated to 3, 4, etc. dimensions

Interpretation of phase plan

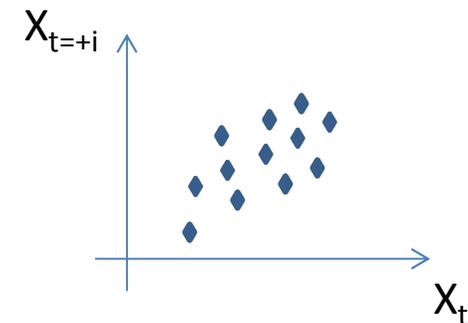
Predictable signals



*Deterministic
(monotonic)*

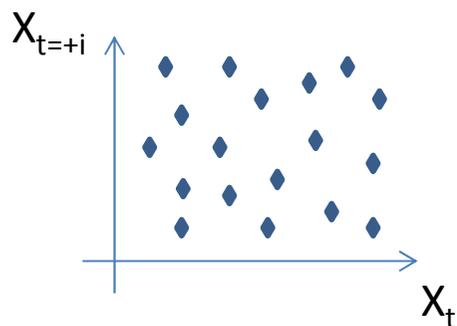


*Deterministic
(Non monotonic)*

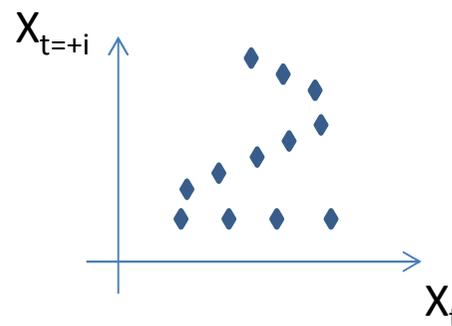


Deterministic+ some noise

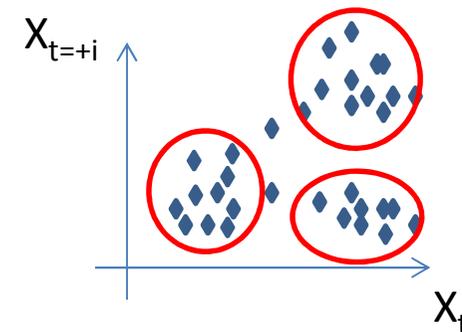
Non-Predictable signals



Random noise



*Non linear
(multiple outcomes)*



*Chaotic signal
(& "strange" attractors)*

Phase Plan Analysis of the Logistic Equation (# embeddings)

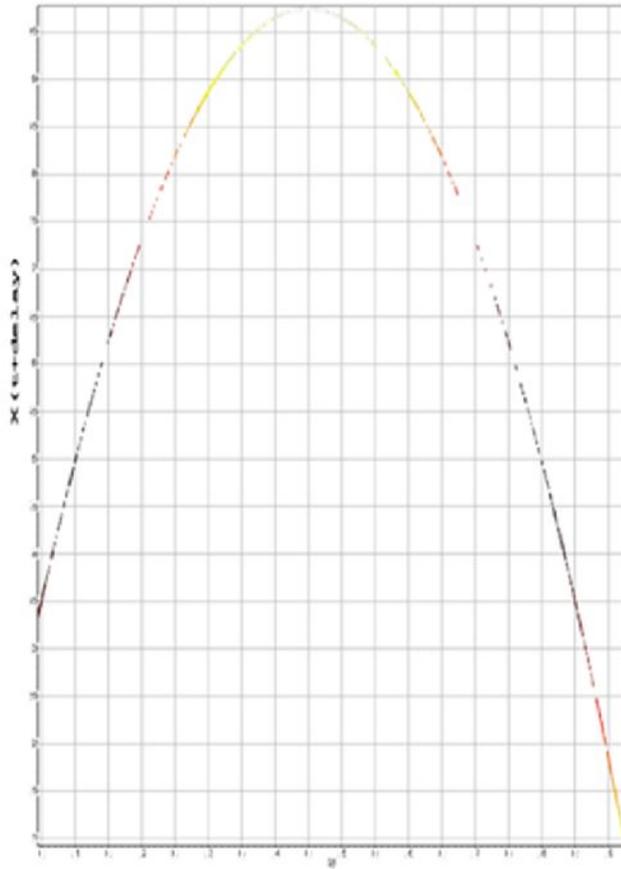


Fig 6a. Phase plot of the Logistic equation. Embedding 01

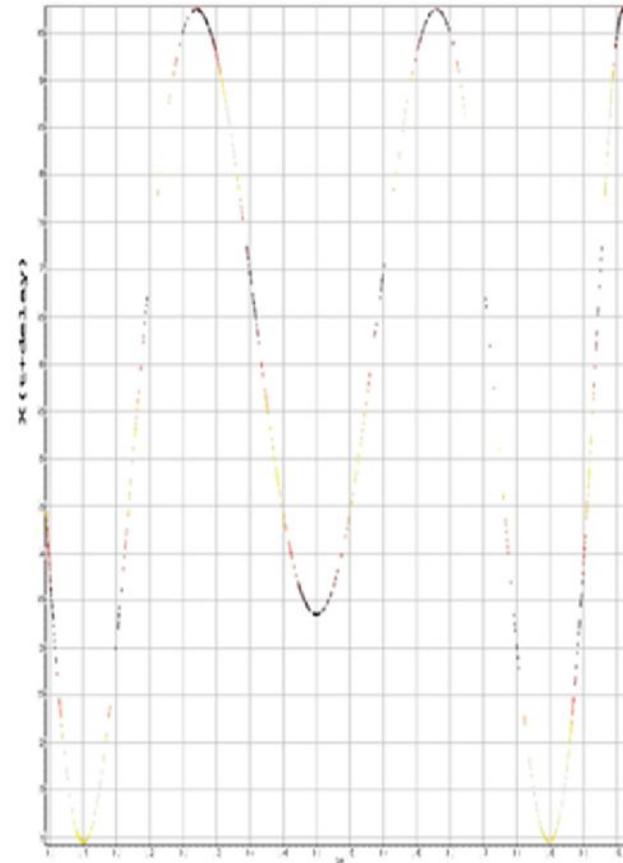


Fig 6b. Phase plot of the Logistic equation. Embedding 03

Phase Plan Analysis of the Logistic Equation (# embeddings) (ctnd)

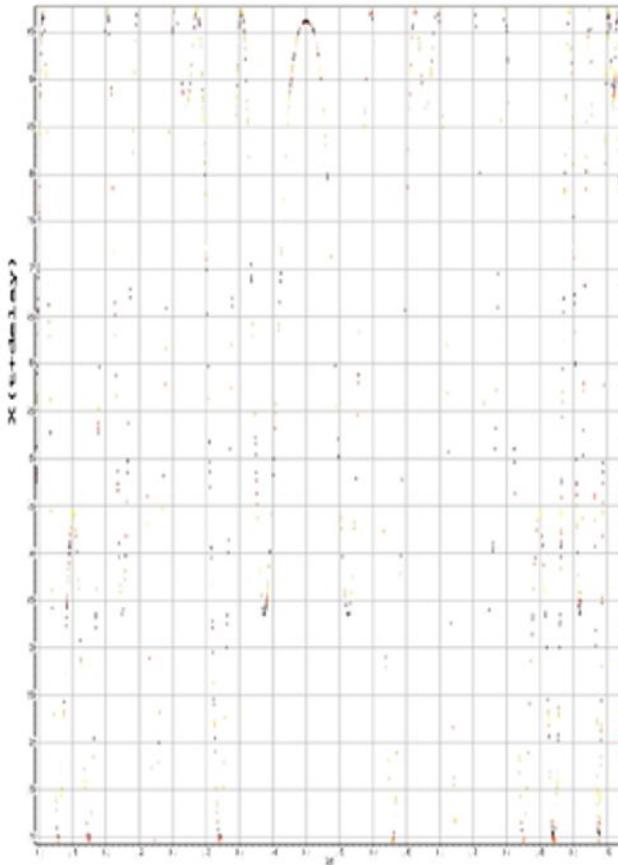


Fig 6c. Phase plot of the Logistic equation. Embedding 06

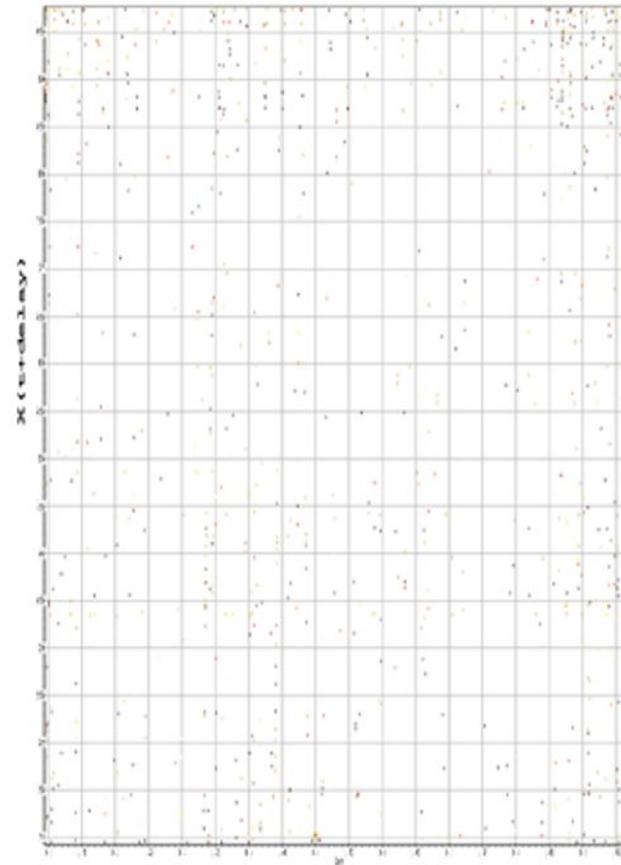
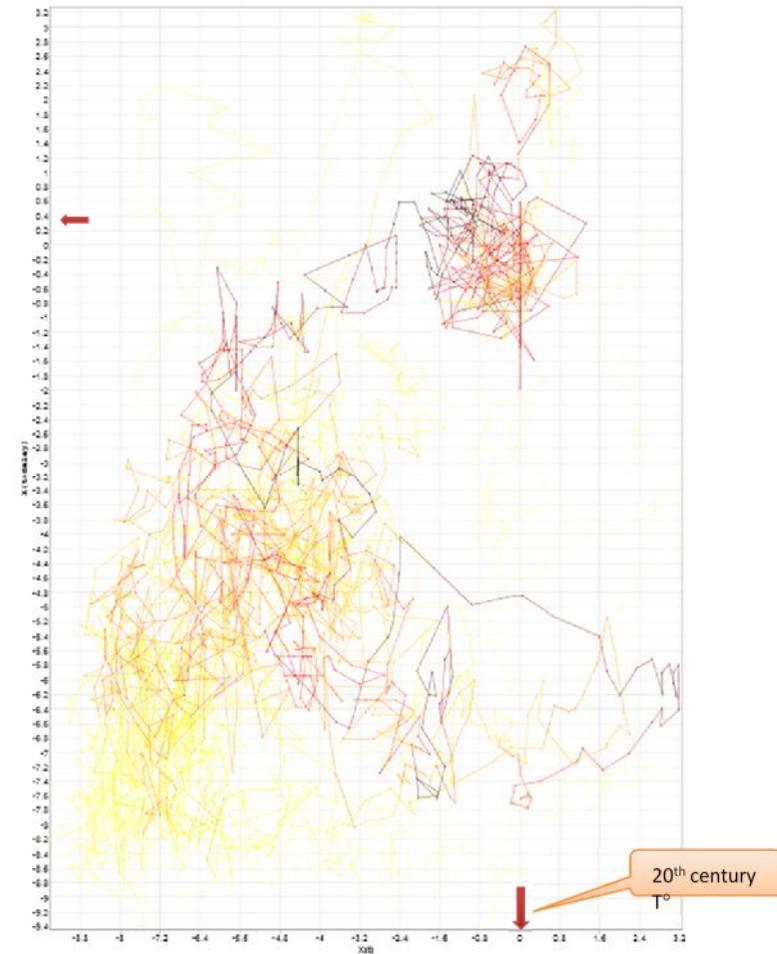
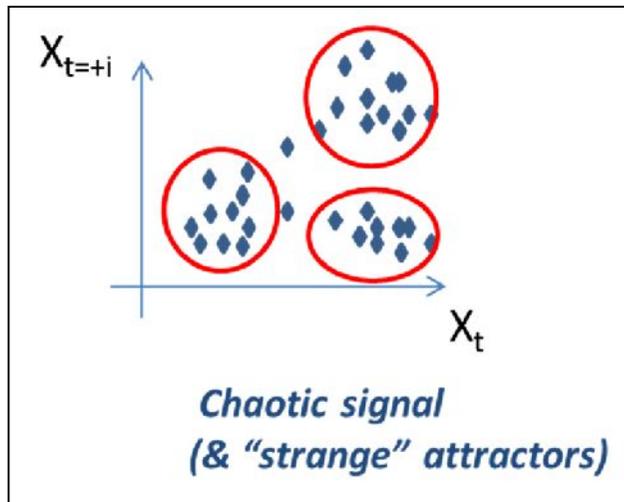


Fig 6d. Phase plot of the Logistic equation. Embedding 10

It is impossible to predict the outcome of the logistic equation 10 steps ahead, only based on the corresponding time series (when one ignores the equation & value of parameters and initial conditions)

Phase diagram of the Vostök data

- The chaotic signature is obvious
- Predictability is very limited



Quantitative Analysis of Phase Space

- **Embedding dimension (ED):** the value of the time shift \mathbf{i} in $X_{t+i} = f(X_t)$
(=> analysis of predictability)

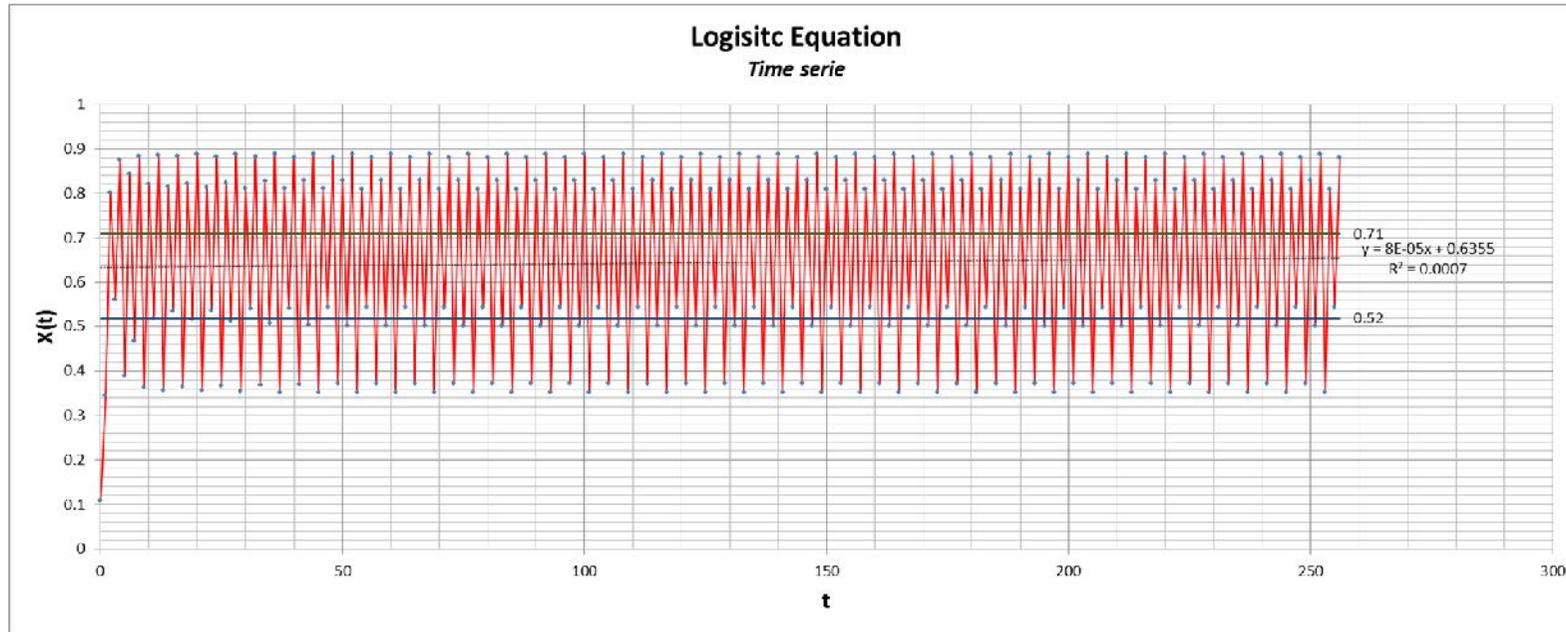
- **Correlation Dimension (CD)**

- $C(\varepsilon)$ = probability that 2 points differ by less than ε in the phase space

$$\lim_{\varepsilon \rightarrow 0} \lim_{C \rightarrow \infty} \left(\frac{\log(C)}{\log(\varepsilon)} \right)$$

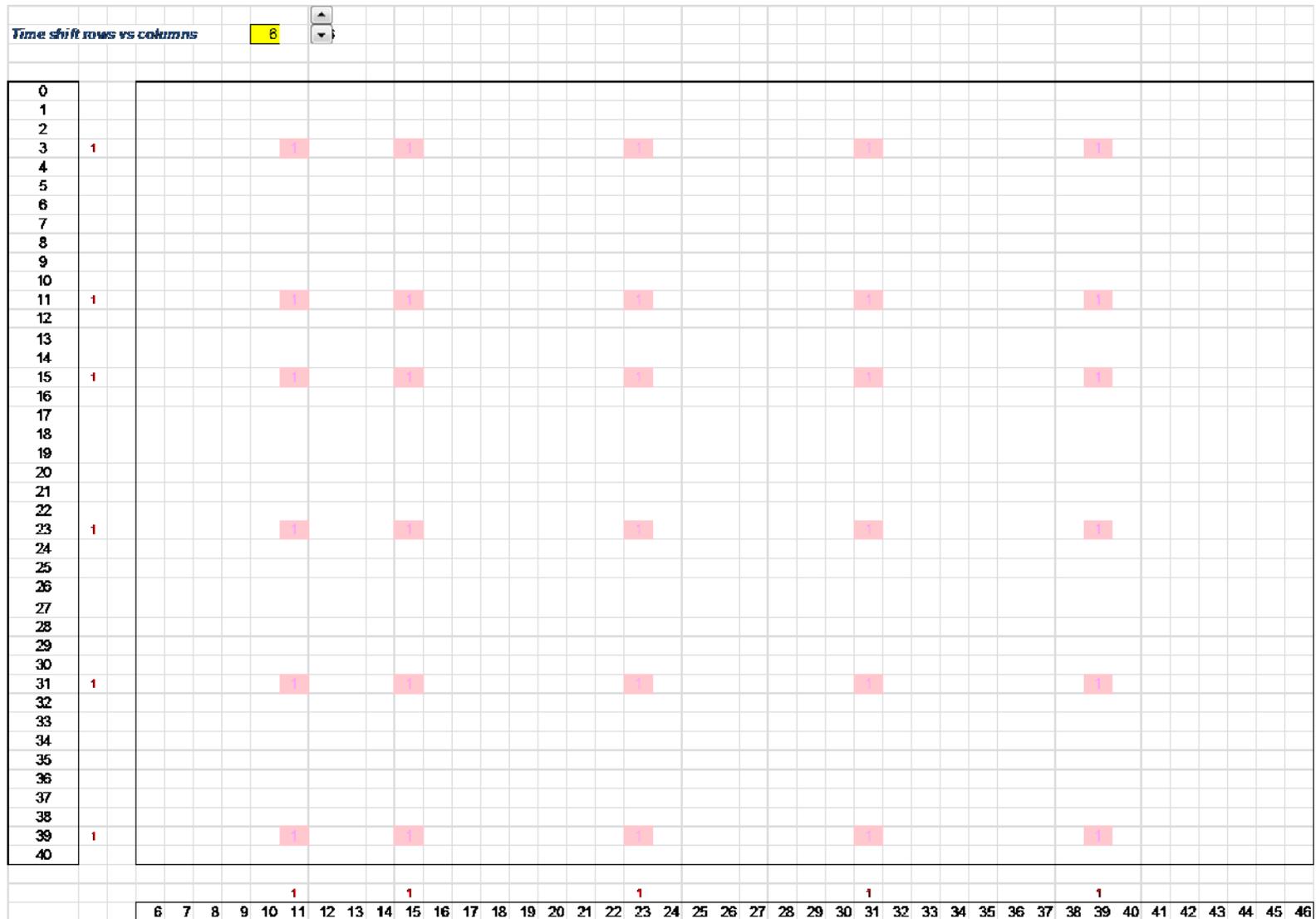
- On Diagonal in graph CD versus ED (embedding dimension) if signal is random
 - Reaches some saturation for periodic or chaotic functions
 - If # integer: indication of a **fractal** dimension
- **False Nearest Neighbour**
 - Stays around 50% if signal is random
 - First minimum gives estimation of most interesting embedding dimension for random & periodic signals
 - **Noise reduction** (# algorithms do exist)
 - **Non parametric time series predictions** (without having to make an hypothesis on the shape of the relation)
 - And many others (*Hurst* coefficients, *Lyapounov* exponents,)

Recurrence Plot: Principle

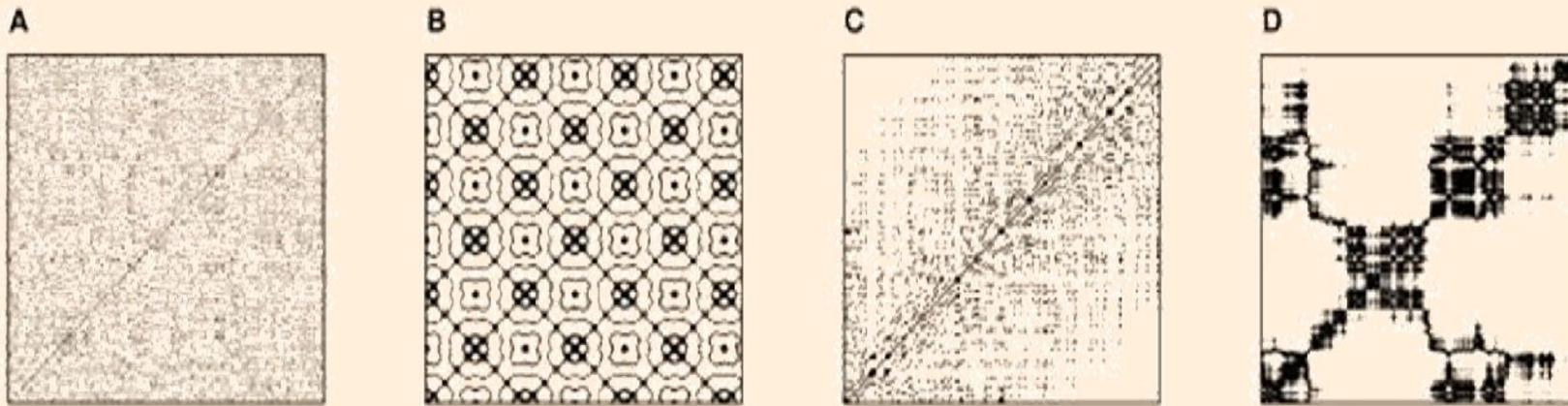


- Checks when the signal falls in a given amplitude window
- Time series is cut in strips of length L
- Each “strip is shifted towards the preceding one by n ”
- Strips are juxtaposed & the “*distances*” between neighbouring points are computed
- Different “distance windows” are superposed using colour coding
- Eventually: Vectors of points (spaced each other along the time series by the embedding dimension) are considered & the “distance” between the vectors is calculated
- Pattern recognition is applied
- Patterns are analysed *qualitatively (visually) & quantitatively*

Recurrence Plot (one window)



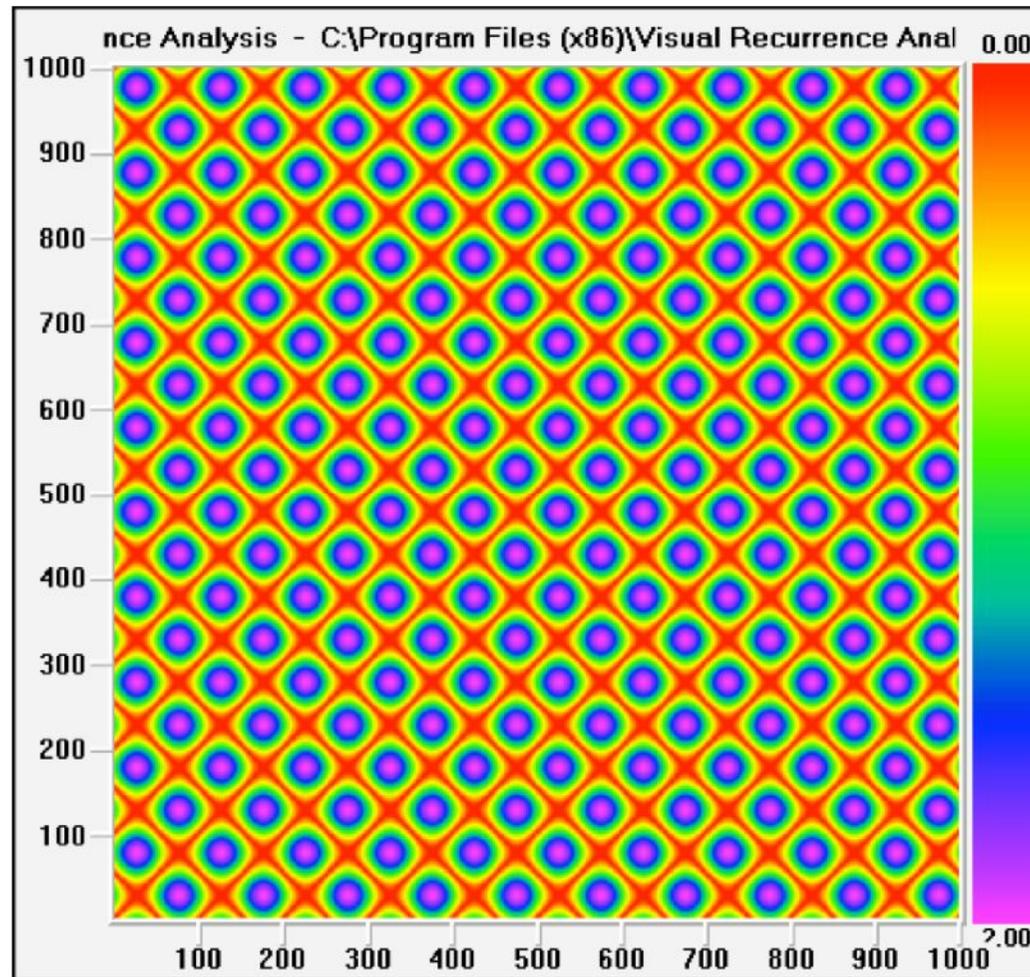
Recurrence Plot Signatures



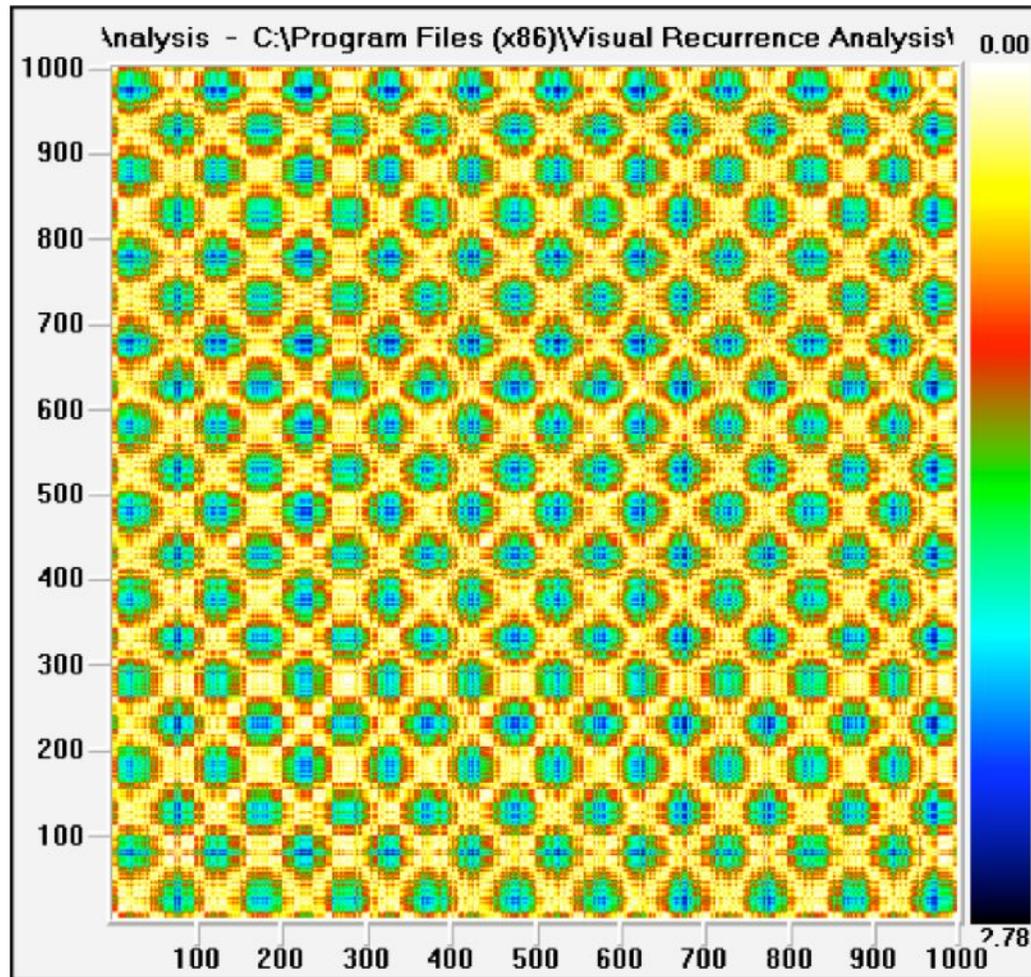
Characteristic typology of recurrence plots: (A) homogeneous (uniformly distributed noise), (B) periodic (super-positioned harmonic oscillations), (C) drift (logistic map corrupted with a linearly increasing term) and (D) disrupted (Brownian motion). These examples illustrate how different RPs can be. The used data have the length 400 (A, B, D) and 150 (C), respectively; no embeddings are used; the thresholds are $\epsilon=0.2$ (A, C, D) and $\epsilon=0.4$ (B).

A vertical-horizontal cross through the diagram = some exceptional event.

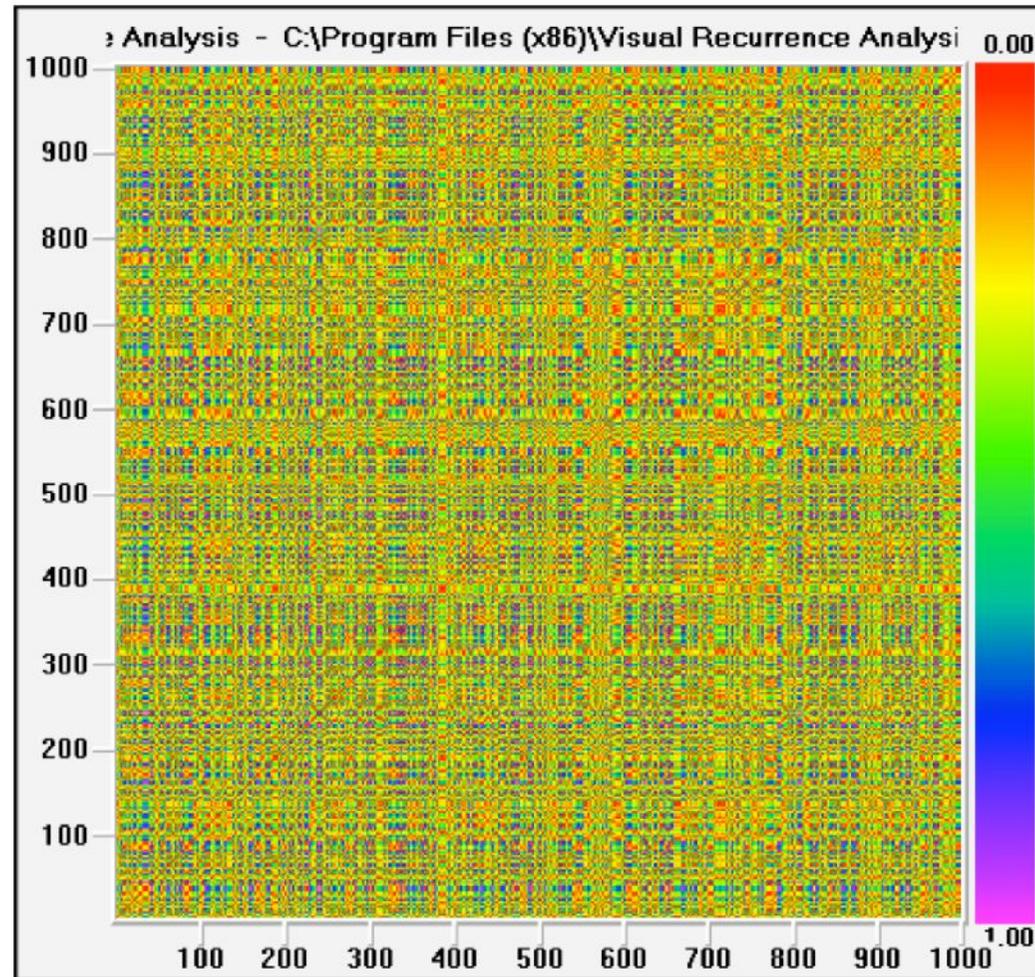
R.P. for a sinusoid



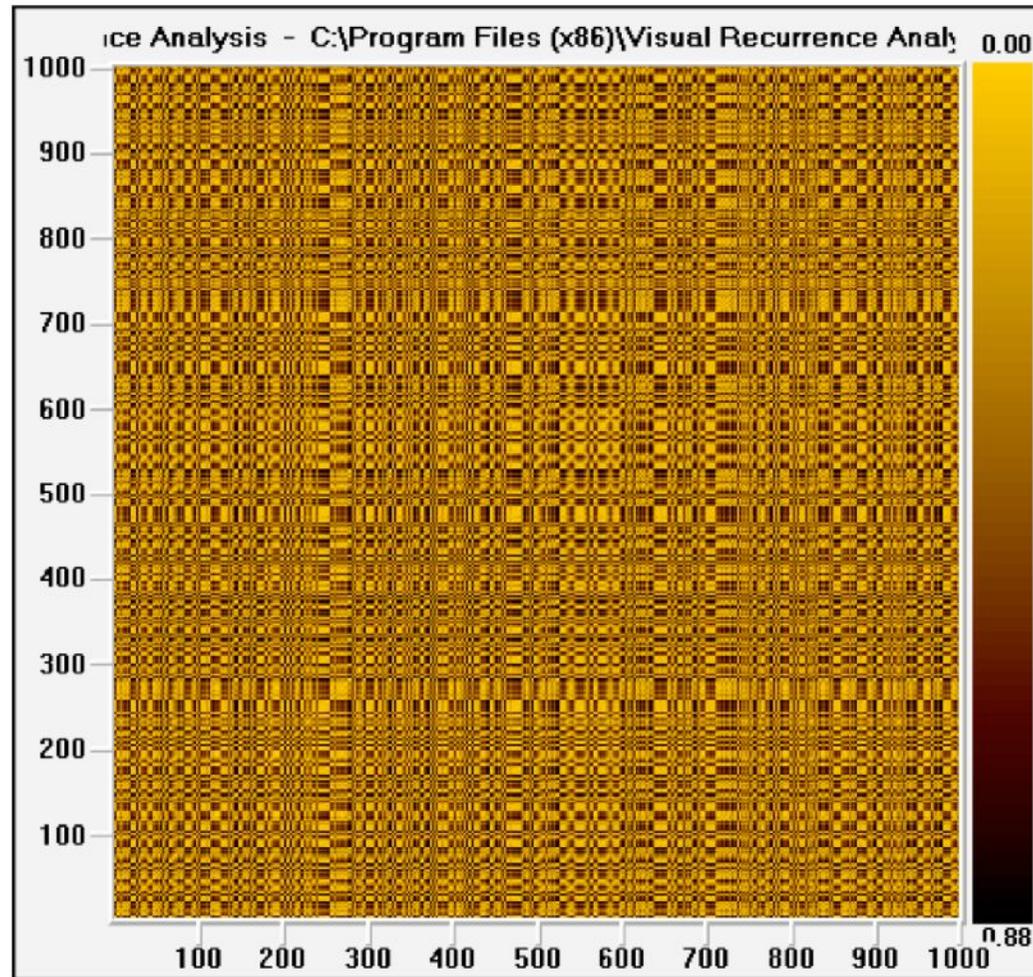
R.P. for Sinusoid + noise



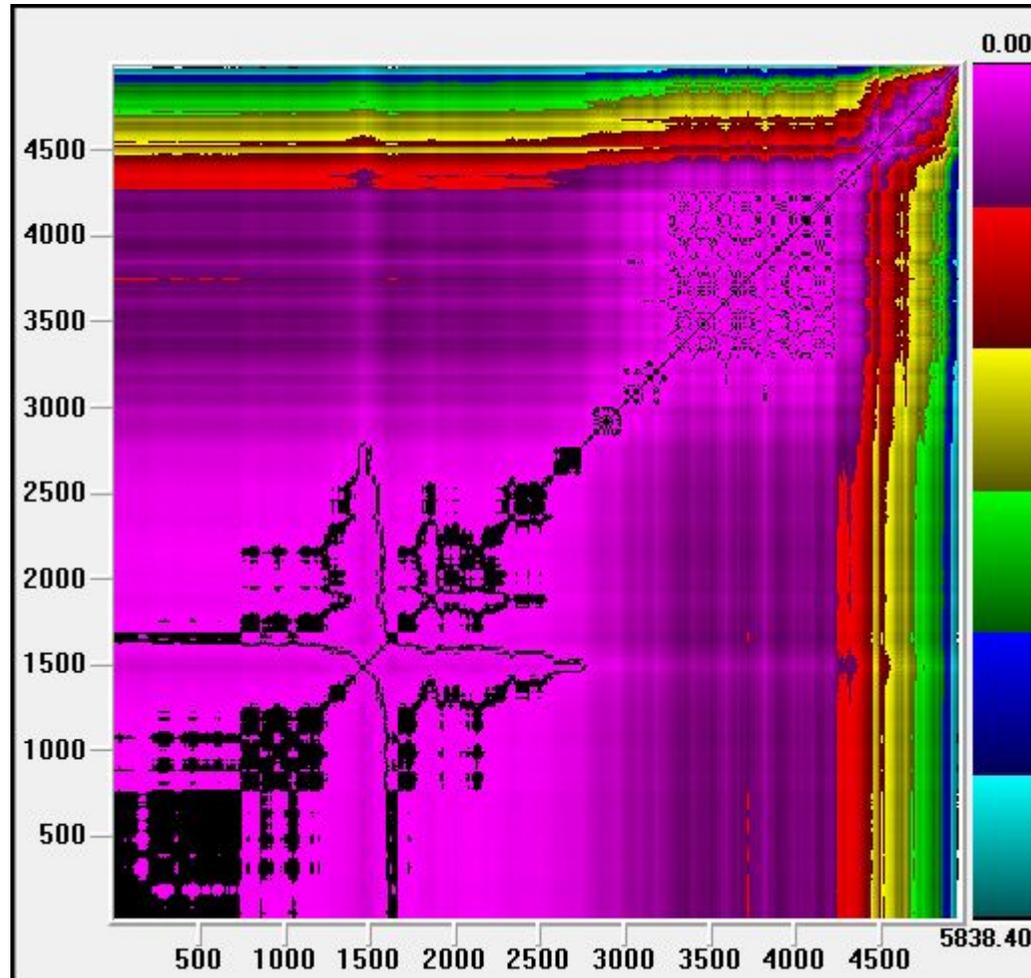
R. P. for a Random Signal



RP for the Logistic Curve

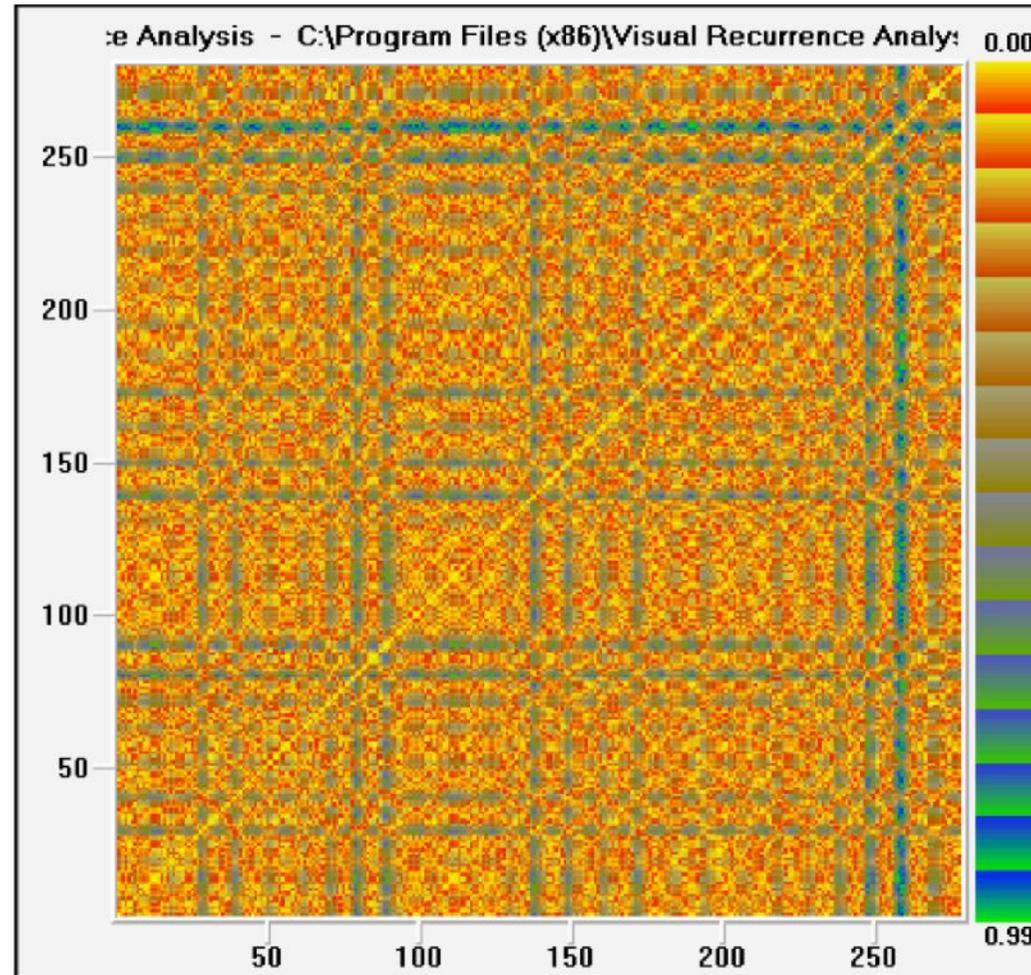


R.P. for Dow Jones

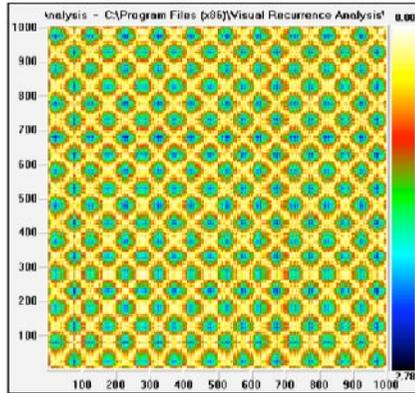


A trend line in time series => “structures” at two ends of the diagonal

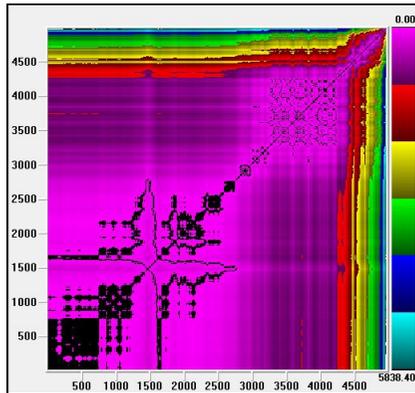
R.P for Sun Spots Number



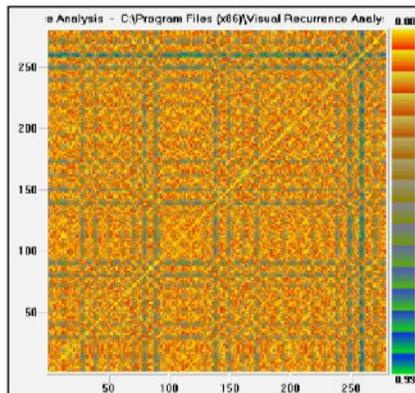
R.P. for Local Temperature Time Series



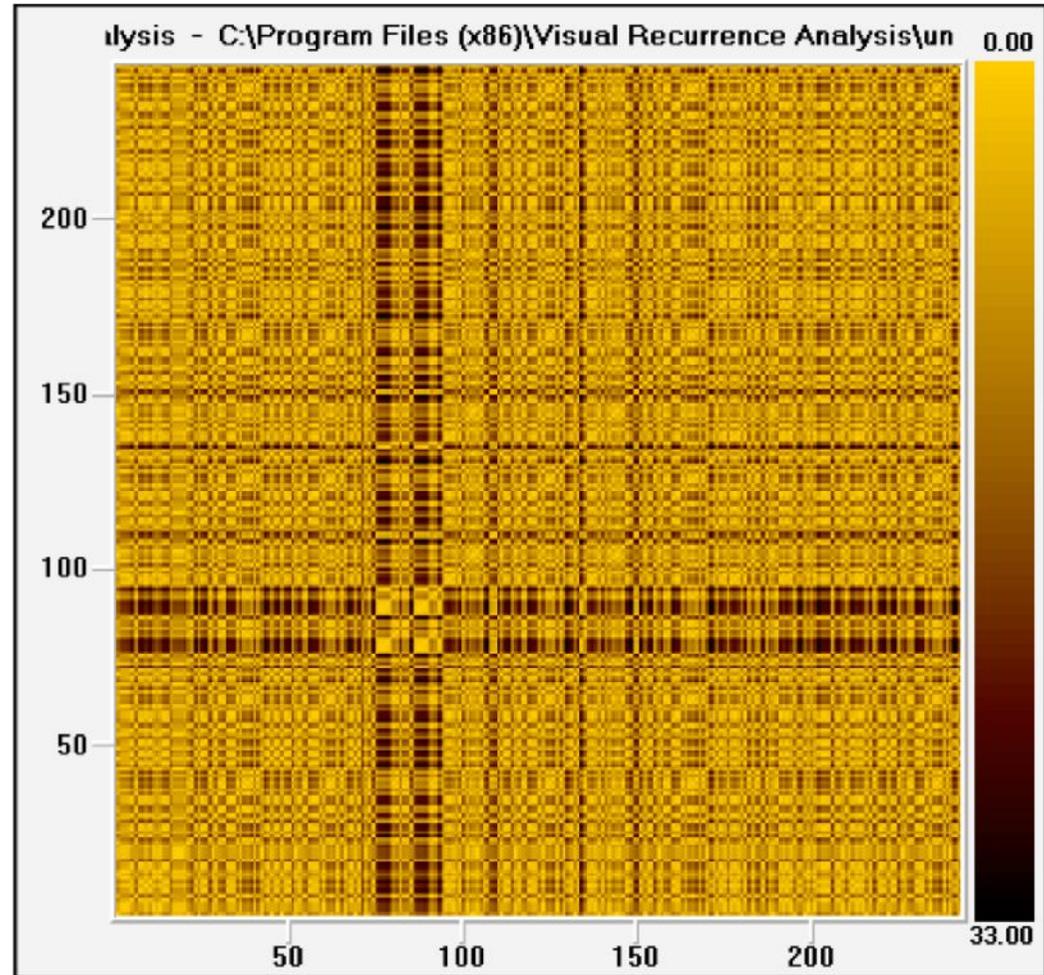
Sinusoid
+ noise



Trend
line



Number
of sun
spots
(chaotic)

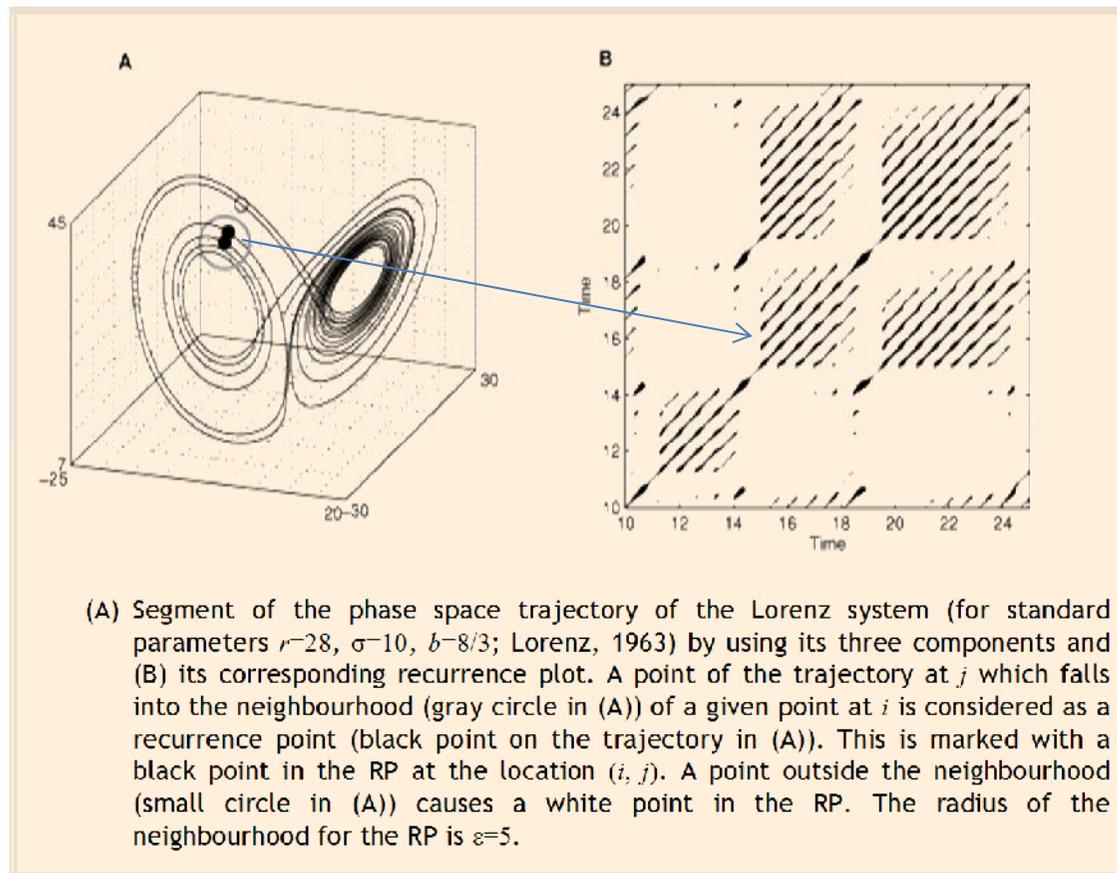


Daily Averaged Temperature in Brussels since 1830
(30 000 points)....**NO TREND....similar to R.P. for sun
spots....Chaotic signature**

Quantitative Analysis of Recurrence Plots

- *Length of vertical signals*: persistence
- *Regular patterns & oblique lines*: periodic signal spaces by $1/4^{\text{th}}$ of a period
- *Length of interrupted oblique lines*: extended of corruption of a periodic signal by noise
- *Size & extend of chaotic patterns & blanks*
- Etc.

Link between Phase Space and Recurrence Plot



WAVELETS ANALYSIS

Principle of Wavelets Analysis

(spectrograms, scalograms, ...)

- Adapted from voice recognition methods
- A signal filtering technique aimed to represent
 - As function of *time* (horizontal axis)
 - The contribution of different *frequencies* (vertical axis) to the *power* of the signal (colour coded third dimension of the graph)
-  ***evolution over time of a Power Spectrum***
(already described).

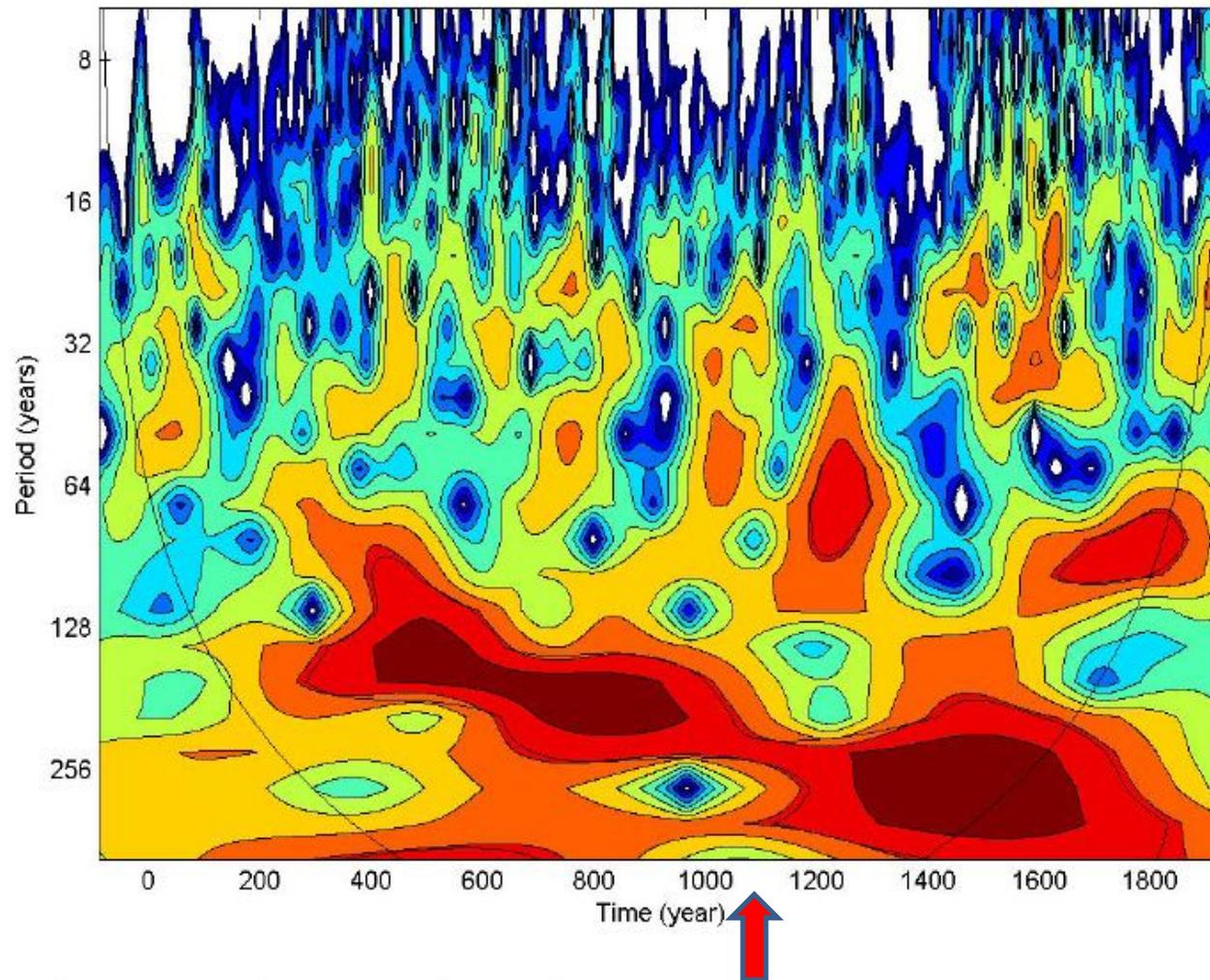
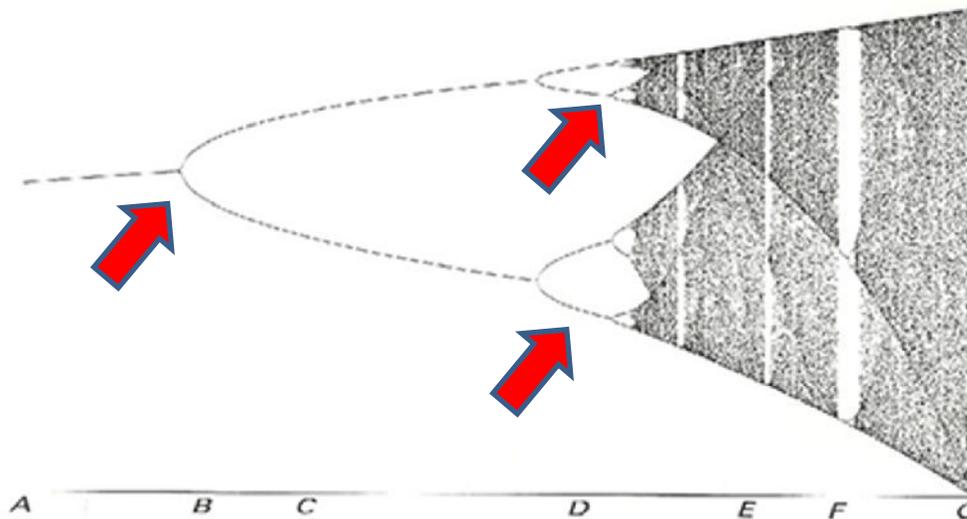


Fig. 4. (color online) Wavelet (Morlet) spectrum [18] of the interpolated SPA record from -90 until 1935 AD. The solid black line from the left to the right top of the Figure is the cone of influence (below the coi the results are not significant). The spectrum shows that the power density between the period of 128 and 256 years is moving with increasing time to lower frequencies. This area is only badly resolved in M6 (see Fig. 3, left panel)

H-J. Ludecke, A. Hempelmann, and C. O. Weiss (2012)

Bifurcations are a signature for chaotic signals

(recall of the bifurcation diagram for the logistic equation)



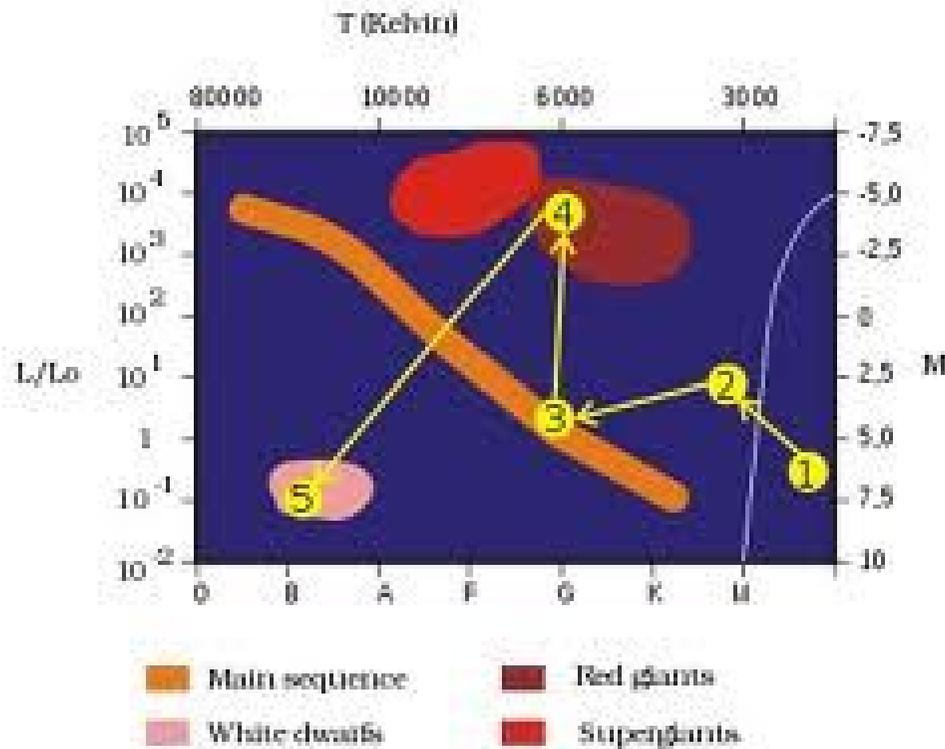
	Order and chaos in the model of restricted growth $x \rightarrow ax(1-x)$
A	$a = 2.9$ single limit point
B	$a = 3.0$ transition to 2-cycle
C	$a = 3.2$ 2-cycle
D	$a = 3.5$ 4-cycle
E	$a = 3.74$ 5-cycle
F	$a = 3.83$ 3-cycle
G	$a = 4.0$ complete chaos

The data of Ludecke et al, obtained from measurements made on stalactites in a Bavarian cave show the progressive (and slow) move of the climate system towards a (less and less predictable) Chaotic State.

A significant bifurcation happened around year 1000.

This is probably due to some astrophysical event (explosion of giant star becoming a supernovae in the crab constellation?)... but surely not due to anthropogenic carbon

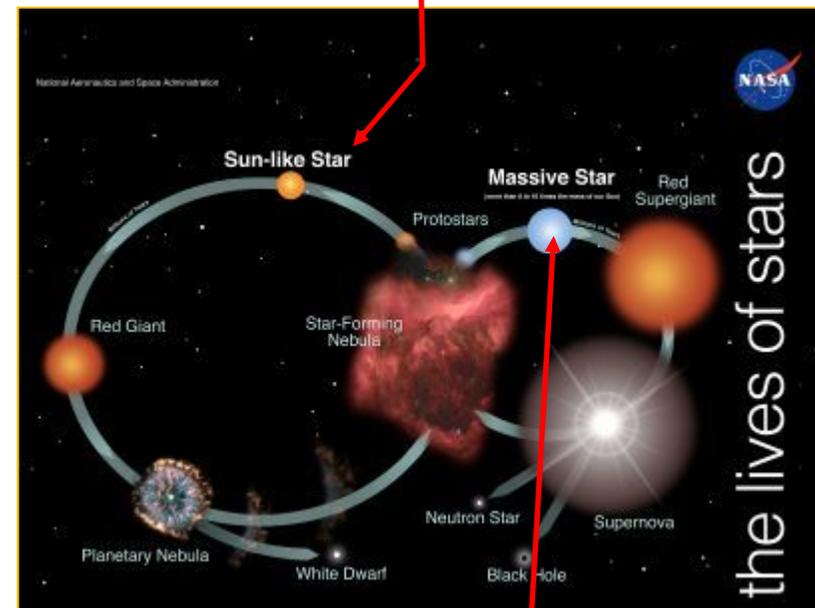
In brief: The fate of stars.....



Evolution of stars in a graph (Log) Relative Irradiance (present Sun =1) versus temperature (°K) .

The Sun (small star) is presently in phase 3 (irradiance =1) & will evolve towards a red giant (4) before exploding into a Nebula inmillions of years(?) before becoming a white dwarf (5)

Small star (Sun) => Giant red => nebula => white dwarf (sequence 1 to 5 , on the left figure)



Massive star => hyper-giant red star => supernova=> Neutronic star + black hole

Size of the Universe....

- Mass of the Sun = 330 000 * earth mass
- Mass Jupiter = 2.5* Σ (mass of all other planets in solar system)
- Etc...

(www.cosmonline.co.uk)

Neither significant electro-magnetic nor significant gravitational influence on:

- earth rotation speed?
- Position of rotation axis?
- Magnetosphere?
- Stresses in magma and tectonic plates (= volcanism)?
- Movement of oceans
- Movement of anticyclones & barometric depressions zones??

10 –Crab Nebula= Results from the Explosion of a giant star in Supernova during year 1054 (observed by Chinese astronoms)

The Universe: Just how big is big?

1. This is Earth
Currently home to some 7 billion human beings and an estimated 8.7 million species of animal and plant life. For the majority of human history Earth was considered the centre of the Universe
Earth: 12,756km

2. Jupiter is the largest planet in our solar system. This gas giant is so enormous that you would have to gather together all the other planets in the solar system and multiply their mass by two and a half times to equal Jupiter's
Jupiter: 142,984km

3. TrES-4 is the largest exoplanet yet discovered. It is about 70 per cent larger than Jupiter but is actually less dense and so has less mass – in fact, it has the density of balsa wood and would quite happily float in water (in a big enough pool)
TrES-4: 228,000km

4. The Sun is enormous (about 330,000 times the mass of Earth). Our local star accounts for more than 99.8 per cent of all the mass in the solar system. Every second, nuclear fusion reactions convert about 700,000 tonnes of hydrogen into helium and energy
Sun: 1,392,000km

5. Aldebaran is an orange giant star that has exhausted its supply of hydrogen. It is about 30-40 times the mass of the Sun. But even this is dwarfed by...
Aldebaran: 61,000,000km

6. KY Cygni is a red giant star that is the largest yet discovered. It measures in at about 1,420 times the Sun's diameter and is about 300,000 brighter
KY Cygni: 2,301,000,000km

7. If KY Cygni was dropped into our **Solar System** it would swallow our Sun and all the planets up to (and including) Saturn. But if we set the boundary of the solar system as being the point at which the heliosphere (the bubble of solar wind extending from the Sun) runs out, it gives KY Cygni a damn good thrashing
Our Solar System: 26,900,000,000km

8. The black hole at the heart of a galaxy called **M87** was recently measured by the Event Horizon Telescope. The innermost orbit of its accretion disk is swirling being sucked into the black hole was found to be some 113 billion km in diameter
Black hole: 113,000,000,000km

9. This is the Cat's Eye Nebula – a huge cloud of gas and dust spat out into space by the dying star at its centre (which is about 10,000 times brighter than our Sun). Despite its size compared to our solar system, it is actually one of the smaller nebula in the Milky Way
Cat's Eye Nebula: 3,780,000,000,000km

10. This is another nebula, called the Crab Nebula. It is the dusty remains of a star that exploded as a supernova, which was spotted by the Chinese in 1054
Crab Nebula: 104,000,000,000,000km

11. A different sort of nebula, the Rosette Nebula is a stellar nursery – colossal cloud of gas in which new stars are born. The mass of the nebula has been estimated at 10,000 solar masses
Rosette Nebula: 1,230,000,000,000,000km

12. This is the Small Magellanic Cloud – a dwarf galaxy that orbits the Milky Way. It is home to about a hundred million stars and has a total mass of about seven billion Suns
Small Magellanic Cloud: 66,200,000,000,000,000km

13. So this is the galaxy we all live in – the Milky Way. It is a middle-weight galaxy that contains between 100-200 billion stars. It has been estimated that there could be some ten billion habitable planets around those stars
Milky Way: 1,140,000,000,000,000,000km

14. This is IC 1101 It is the largest galaxy yet discovered. It is about 50 times larger than the Milky Way and is home to about 100 trillion stars (about the same as the total number of cells in your body)
IC 1101: 53,000,000,000,000,000,000,000km

15. The Virgo Supercluster is a supercluster of galaxies (including the Milky Way). It contains at least 100 groups of galaxies with each group containing at least 70 galaxies
Virgo Supercluster: 1,040,000,000,000,000,000,000km

16. This map of Local Universe (made by the MASS Redshift Survey) covers the entire visible sky. Visible in the image are more than 300 million stars and more than 1.5 million galaxies
Local Universe: 24,600,000,000,000,000,000,000km

17. The Observable Universe encompasses the region of the Universe that we can in theory see from Earth – all the stars and galaxies whose light has been able to reach Earth in the 13.7-billion years since the Big Bang
Observable Universe: 880,000,000,000,000,000,000,000,000km

**MORE GENERAL CONSIDERATIONS
& CONCLUSIONS**

“ The Blind Men and the Elephant ”

an Hindu fable

*It was six men of Hindustan
To learning much inclined,
Who went to see the Elephant
(Though all of them were blind),
That each by observation
Might satisfy his mind*

The **First** approached the Elephant,
And happening to fall
Against his **broad and sturdy side**,
At once began to bawl :
“ God bless me ! – but the Elephant
Is very like a **wall** ! ”
The **Second**, feeling of **the tusk**,
Cried : “ Ho ! – what have we here
So very round and smooth and sharp ?
To me ‘t is mighty clear
This wonder of an Elephant
Is very like a **spear** ! ”
The **Third** approached the animal,
And happening to take
The squirming **trunk** within his hands,
Thus boldly up and spake :
“ I see, ” quoth he, “ the Elephant
Is very like a **snake** ! ”
The **Fourth** reached out his eager hand,
And felt about the **knee**.
“ What most this wondrous beast is like
Is mighty plain, ” quoth he ;
“ ‘T is clear enough the Elephant
Is very like a **tree** ! ”



Importance of:

- Multidisciplinary Dialogue
- Reconstructing the complete picture (systemic thinking)

The **Fifth**, who chanced to touch the **ear**,
Said : “ E’en the blindest man
Can tell what this resembles most ;
Deny the fact who can,
This marvel of an Elephant
Is very like a **fan** ! ”
The **Sixth** no sooner had begun
About the beast to grope,
Then, seizing on the swinging **tail**
That fell within his scope,
“ I see, ” quoth he, “ the Elephant
Is very like a **rope** ! ”

And so these men of Hindustan
Disputed loud and long,
Each in his own opinion
Exceeding stiff and strong,
Though each was partly in the right,
And all were in the wrong !
So, oft in theologic wars
The disputants, I ween,
**Rail on in utter ignorance
Of what each other mean,
And prate about an Elephant
Not one of them has seen !**

« *The Science is Settled* »???

Some of the Key Near-term Science Challenges in Climate and Large Scale Dynamics

- *Modelling and prediction of organized tropical convection'*
- *Tropical-extratropical interactions; storm tracks and moisture transports*
- *Role of atmosphere-ocean interactions in intra-seasonal variability*
- *Systematic zonal flow variations: mechanisms and predictive implications*
- *Predictability of tropospheric wave guides and baroclinic wave packets*
- *Troposphere-stratosphere interactions; modelling and potential predictability*
- *Variability of climate modes beyond ENSO and MJO*
- *Effects of global ocean conditions, e.g. tropical Indian and Atlantic Oceans*
- *Effects of land surface processes*
- *Warm season climate system and its predictability*
- *Potential implications of climate change*

Attribution problems

- ***Type 1:*** *How do you disentangle natural variability of the climate/earth system from 'forced' change?*
- ***Type 2:*** *Given that the climate system is changing due to anthropogenic effects, how do you attribute particular events to the change? What are the conditional PDFs?*

Michael Morgan paper presented at [UCAR](#) (University Corporation for Atmospheric Sciences) Annual Member's Meeting (Boulder, USA, [November 2012](#)).

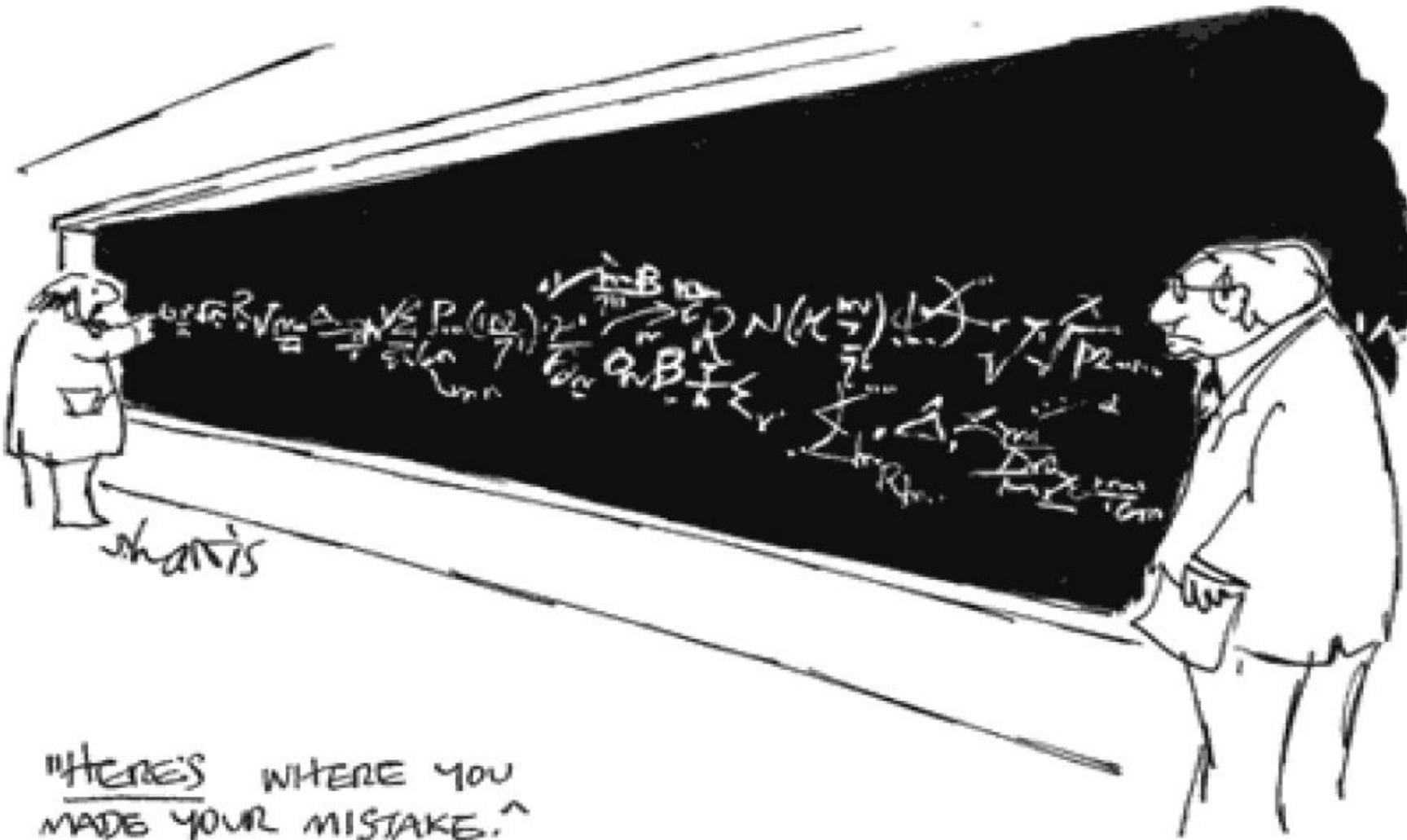
UCAR is the governing body of the National Centre for Atmospheric Research (NCAR).

Conclusions

- **Linear analysis** of (climate) time series are affected by serious drawbacks, especially when the time window considered is too small and when data exhibit some oscillatory component.
- The climate system is slowly evolving with time towards **chaos**, which makes it difficult to predict on the long term
- As transition to chaos happens through bifurcations (creation of harmonics of a fundamental period), the best possible forecasting method, on the short term is by Fourier analysis (sum of sinusoids)
- This trend towards a chaotic state started many centuries before anthropogenic carbon emissions became significant
- The climate system is much more complicated than described by IPCC models, so far.
- Complex systems may create **synchronisation (or phase locking)** between oscillating phenomena, by **mutual** intermittent influence, but without any formal causal (continuous) links between them
- **The master clock** could be of astrophysical origin (conjunction of planets, influence of supernovae, etc.) & its signals are probably of combined gravitational and magnetic nature

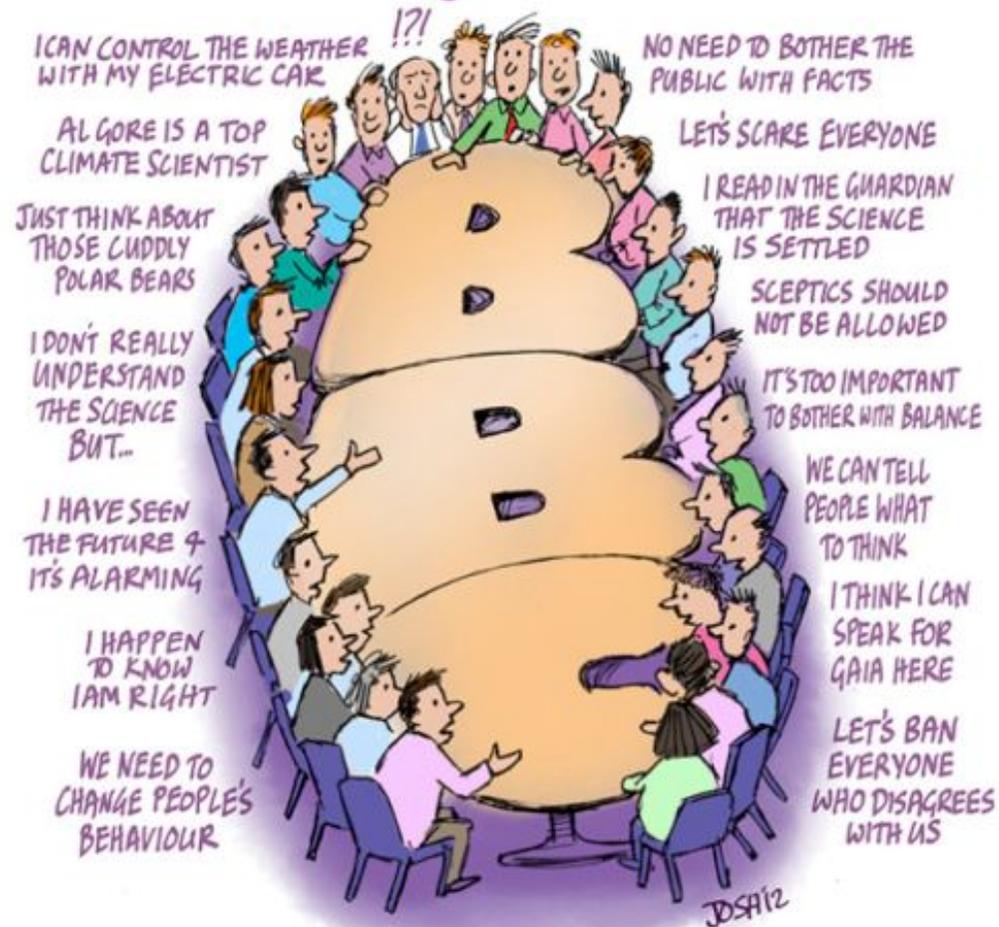
THAT'S (QUITE) ALL FOLKS

Initially, something went wrong with the IPCC models



What happens in Doha?

28GATE



WAYBACK WHEN
THEY DECIDED WHAT
WE SHOULD THINK

It's that same old song...







"Dreaming of a White Christmas!"

© Seppo Leinonen
www.seppo.net

Fortunately the science is not yet settled ... and we have a lot of things to debate on.... And meet again



THANK YOU FOR YOUR ATTENTION

Source data

CLIMATIC INDICATORS

Climatic Indicators

PNA	Pacific North American Index* :From NOAA Climate Prediction Center (CPC)
EP/NP	East Pacific/North Pacific Oscillation :From NOAA Climate Prediction Center (CPC). This index replaces the old EP index which is no longer maintained by CPC.
WP	Western Pacific Index* From NOAA Climate Prediction Center (CPC)
NAO	North Atlantic Oscillation* From NOAA Climate Prediction Center (CPC)
NAO (Jones)	North Atlantic Oscillation From CRU Hurrell, J.W., 1995: Decadal trends in the North Atlantic Oscillation and relationships to regional temperature and precipitation. Science 269, 676-679. Jones, P.D., Jónsson, T. and Wheeler, D., 1997: Extension to the North Atlantic Oscillation using early instrumental pressure observations from Gibraltar and South-West Iceland. Int. J. Climatol. 17, 1433-1450.
SOI*	Southern Oscillation Index From NOAA Climate Prediction Center (CPC)
Nino 3*	Eastern Tropical Pacific SST (5N-5S,150W-90W) From NOAA Climate Prediction Center (CPC)
BEST* longer version	Bivariate ENSO Timeseries Calculated from combining a standardized SOI and a standardized Nino3.4 SST timeseries. Note that different SST dataset (Hadley SST) is now used to calculate Nino 3.4 timeseries. This replaces the GISST dataset. Most recent data is based on the NOAA OI V2 SST dataset. PSD
TNA	Tropical Northern Atlantic Index* Anomaly of the average of the monthly SST from 5.5N to 23.5N and 15W to 57.5W. GISST and NOAA OI 1x1 datasets are used to create index. Climatology is 1951-2000. Enfield, D.B., A.M. Mestas, D.A. Mayer, and L. Cid-Serrano, 1999: How ubiquitous is the dipole relationship in tropical Atlantic sea surface temperatures? JGR-O, 104, 7841-7848. AOML and PSD
TSA	Tropical Southern Atlantic Index* Anomaly of the average of the monthly SST from Eq-20S and 10E-30W. GISST and NOAA OI 1x1 datasets are used to create index. Climatology is 1951-2000. Enfield, D.B., A.M. Mestas, D.A. Mayer, and L. Cid-Serrano, 1999: How ubiquitous is the dipole relationship in tropical Atlantic sea surface temperatures? JGR-O, 104, 7841-7848. AOML and PSD
WHWP	Western Hemisphere warm pool* Monthly anomaly of the ocean surface area warmer than 28.5°C in the Atlantic and eastern North Pacific. Climatology is 1951-2000. Wang, C., and D.B. Enfield, 2001: The tropical Western Hemisphere warm pool, Geophys. Res. Lett., 28, 1635-1638. AOML and PSD
ONI	Oceanic Nino Index From NOAA Climate Prediction Center (CPC). Three month running mean of NOAA ERSST.v2 SST anomalies in the Nino 3.4 region (5N-5S, 120-170W), based on the 1971-2000 base period. Time Series is a newer version from source!
MEI	Multivariate ENSO Index (MEI)* From PSD . Time series is bimonthly so the Jan value represents the Dec-Jan value and is centered between the months. Details and current values are at Dr Wolter's website . Reference: Wolter, K., and M.S. Timlin, 1998: Measuring the strength of ENSO - how does 1997/98 rank? Weather, 53, 315-324.

Climatic Indicators (1)

MEI	Multivariate ENSO Index (MEI)* From PSD. Time series is bimonthly so the Jan value represents the Dec-Jan value and is centered between the months. Details and current values are at Dr Wolter's website. Reference: Wolter, K., and M.S. Timlin, 1998: Measuring the strength of ENSO - how does 1997/98 rank? <i>Weather</i> , 53, 315-324.
Nino 1+2	Extreme Eastern Tropical Pacific SST *(0-10S, 90W-80W) From CPC
Nino 4	Central Tropical Pacific SST *(5N-5S) (160E-150W) From CPC
Nino 3.4	East Central Tropical Pacific SST *(5N-5S)(170-120W) From CPC
PDO	Pacific Decadal Oscillation is the leading PC of monthly SST anomalies in the North Pacific Ocean. UPDATED: Using data from 1948 to 2002. Details and more information are available.
NOI	Northern Oscillation Index is an index of climate variability based on the difference in SLP anomalies at the North Pacific High and near Darwin Australia. Schwing, F.B., T. Murphree, and P.M. Green. 2002. The Northern Oscillation Index (NOI): a new climate index for the northeast Pacific. <i>Progress in Oceanography</i> 53: 115-139. The time series and more information are available.
NP	North Pacific pattern is the area-weighted sea level pressure over the region 30N-65N, 160E-140W. Time series source Trenberth and Hurrell (1994): <i>Climate Dynamics</i> 9:303-319.
TNI (Trans-Niño Index)	Indices of El Niño evolution: Kevin E. Trenberth and David P. Stepaniak: <i>J. Climate</i> , 14 , 1697-1701. calculated at PSD. for longer timeseries, go to http://www.esrl.noaa.gov/psd/gcos_wgsp/Timeseries/TNI/
Trend	A linear time series (1,2,3,...). NOT the linear trend of the variable
Hurricane activity	(Updated to 2003) Monthly totals Atlantic hurricanes and named tropical storms Each month has the total number of hurricanes or named tropical storms in that month in the Atlantic region. These values are from Unisys at http://weather.unisys.com/hurricane/atlantic/ who obtained them from Colorado State/Tropical Prediction Center. I computed the number of hurricanes that begin in each month. Note that the hurricane might extend to the next month but won't be listed there. Their webpage should be read for a more complete description and attribution.
AO	Note, values are now from CPC as they update their data through the present From CPC: The loading pattern of AO (AAO) is defined as the first leading mode from the EOF analysis of monthly mean height anomalies at 1000-hPa (NH) or 700-hPa (SH). Note that year-round monthly mean anomaly data has been used to obtain the loading patterns. Since the AO and AAO have the largest variability during the cold season (variance of AO/AAO), the loading patterns primarily capture characteristics of the cold season patterns. Daily and monthly AO (AAO) indices are constructed by projecting the daily and monthly mean 1000-hPa (700-hPa) height anomalies onto the leading EOF mode. Both time series are normalized by the standard deviation of the monthly index (1979-2000 base period). Since the loading pattern of AO (AAO) is obtained using the monthly mean height anomaly dataset, the index corresponding to each loading pattern becomes one when it is normalized by the standard deviation of the monthly index. Values and description

Climatic Indicators (2)

AAO	<p>Antarctic Oscillation.</p> <p>Values and references Data from CPC</p>
Pacific Warmpool	<p>1st EOF of SST (60e-170E, 15S-15N) SST EOF, all months</p> <p>GISST 1948-1949 Reconstructed Reynolds 1950-1981 OI 1982-present</p> <p>Reference: Martin P. Hoerling (personal communication)</p>
Tropical Pacific SST EOF	<p>1st EOF of SST 20N-20S, 120E-60W</p> <p>GISST 1948-1949 Reconstructed Reynolds 1950-1981 OI 1982-present</p> <p>Reference: Martin P. Hoerling, Arun Kumar, and Taiyi Xu, 2001: Robustness of the nonlinear climate response to ENSO's extreme phases. <i>Journal of Climate</i>, Vol.14, No.6, 1277-1293</p>
Atlantic Tripole SST EOF	<p>1st EOF of SST 10N-70N, 0-80W</p> <p>GISST 1948-1949 Reconstructed Reynolds 1950-1981 OI 1982-present</p> <p>Deser, Clara, Michael S. Timlin, 1997: Atmosphere-Ocean Interaction on Weekly Timescales in the North Atlantic and Pacific. <i>Journal of Climate</i>: Vol. 10, No. 3, pp.393-408.</p>
Atlantic multidecadal Oscillation Long Version	<p>AMO, unsmoothed</p> <p>Note: this index is newly computed from a new dataset. Please use it and note that it supersedes the old indices. The data is calculated from the Kaplan SST. See the AMO webpage for more details.</p> <p>Enfield, D.B., A. M. Mestas-Nunez and P.J. Trimble, 2001: The Atlantic multidecadal oscillation and it's relation to rainfall and river flows in the continental U.S.. <i>Geophysical Research Letters</i>, Vol. 28, 2077-2080.</p>

Climatic Indicators (3)

Atlantic Meridional Mode	<p>AMM</p> <p>Note: this index is newly available computed from a new dataset. See the AMM webpage for more details.</p> <p>2004 Chiang, J. C. H., and D. J. Vimont: Analogous meridional modes of atmosphere-ocean variability in the tropical Pacific and tropical Atlantic. <i>J. Climate</i>, 17(21), 4143-4158.</p>
North Tropical Atlantic Index (NTA)	<p>NTA: North Tropical Atlantic SST Index</p> <p>(Definition slightly changed: old version available). The timeseries of SST anomalies averaged over 60W to 20W, 6N to 18N and 20W to 10W, 6N to 10N map. Data is obtained from the COADS dataset for 1951-1991 and NCEP afterwards. Anomalies were calculated relative to the 1951-2000 climatology, smoothed by three months running mean procedure and projected onto 20 leading EOFs. Month of data is the center of the 3 months that are smoothed. More information and the indexes forecasted values are available.</p> <p>Penland, C., and L. Matrosova, 1998: "Prediction of tropical Atlantic sea surface temperatures using Linear Inverse Modeling," <i>J. Climate</i>, March, 483-496 pp.</p>
Caribbean Index (CAR)	<p>CAR: Caribbean SST Index</p> <p>The timeseries of SST anomalies averaged over the the Caribbean. Data is obtained from the COADS dataset for 1951-1991 and NCEP after. Anomalies were calculated relative to the 1951-2000 climatology, smoothed by three months running mean procedure and projected onto 20 leading EOFs. More information and the indexes forecasted values are available.</p> <p>Penland, C., and L. Matrosova, 1998: "Prediction of tropical Atlantic sea surface temperatures using Linear Inverse Modeling," <i>J. Climate</i>, March, 483-496 pp.</p>
Atlantic multidecadal Oscillation Long Version	<p>AMO, smoothed</p> <p>Note: this index is newly computed from a new dataset. Please use it and note that it supersedes the old indices. The data is calculated from the Kaplan SST. See the AMO webpage for more details.</p> <p>Enfield, D.B., A. M. Mestas-Nunez and P.J. Trimble, 2001: The Atlantic multidecadal oscillation and its relation to rainfall and river flows in the continental U.S.. <i>Geophysical Research Letters</i>, Vol. 28, 2077-2080.</p>
QBO	<p>Quasi-Biennial Oscillation*. Calculated at PSD (from the zonal average of the 30mb zonal wind at the equator as computed from the NCEP/NCAR Reanalysis).</p>
Globally Integrated Angular Momentum	<p>Globally Integrated Angular Momentum*</p> <p>Note that time series is scaled by 1e25. Values are 3-month running means except for the last month which is a 2-month average.</p> <p>Weickmann, K.M., W.A. Robinson and M.C. Penland, 2000: Stochastic and oscillatory forcing of global atmospheric angular momentum. <i>J. Geophys. Res.</i>, 105, D12, 15543-15557.</p>

Climatic Indicators (4)

ENSO precipitation index	<p><i>ENSO precipitation index</i></p> <p>http://precip.gsfc.nasa.gov/ESPtable.html Please cite "ENSO Indices Based on Patterns of Satellite-Derived Precipitation" Curtis and Adler in <i>J. of Climate</i>, 13,2786 (2000). Time series that uses rainfall data in the Tropical Pacific to describe ENSO events.</p>
Central Indian Precipitation (core monsoon region)	<p><i>Central Indian Precipitation</i></p> <p>http://www.tropmet.res.in/ Please cite the Indian Institute of Tropical Meteorology. CORE-MONSOON INDIA RAINFALL (1871-1999) 7 SUB 776,942 SQ.KM.</p>
Sahel rainfall	<p><i>Sahel Standardized Rainfall (20-8N, 20W-10E)</i></p> <p>http://jisao.washington.edu/data_sets/sahel/ From Mitchell: The averaging region is based on the rotated principal component analysis of average June through September African rainfall presented in Janowiak (1988, J. Climate, 1, 240-255). Stations within 20-8N, 20W-10E are obtained from the National Center for Atmospheric Research World Monthly Surface Station Climatology (WMSSC), and 14 retained which had complete or almost complete records for 1950-93. See link for stations.</p>
SW Monsoon Region rainfall	<p><i>Sahel Area averaged precipitation for Arizona and New Mexico</i></p> <p>Calculated using NCDC's climate division dataset. Monthly precipitation values for each of the climate divisions in Arizona and New Mexico are averaged to produce a single monthly value. Reference: personal communication, Catherine Smith. Also, NCDC, 1994, Time Bias Corrected Divisional Temperature-Precipitation-Drought Index. Documentation for dataset TD-9640. Available from DBMB, NCDC, NOAA, Federal Building, 37 Battery Park Ave. Asheville, NC 28801-2733. 12pp.</p>
Northeast Brazil Rainfall Anomaly	<p><i>Northeast Brazil Rainfall Anomaly</i></p> <p>http://jisao.washington.edu/data_sets/brazil/ From Mitchell: The northeast Brazil rainfall index is calculated from data for Fortaleza (3.7S, 38.5W) and Quixeramobim (5.3S, 39.3W) Brazil obtained from the NCAR World Monthly Surface Station Climatology. Climatological mean is for 1950-79.</p>
Solar Flux (10.7cm)	<p><i>Solar Flux (10.7cm)*</i></p> <p>http://www.ngdc.noaa.gov/nndc/struts/results?op_0=eq&v_0=Penticton_Observed&t=102827&s=4&d=8&d=22&d=9 For NGDC. t To cite, "The 10.7cm Solar Flux Data are provided as a service by the National Research Council of Canada". They would appreciate a preprint or at least a reference if you use the data (URL is http://www.drao.nrc.ca/index_eng.shtml). Time series is ftp://ftp.ngdc.noaa.gov/STP/SOLAR_DATA/SOLAR_RADIO/FLUX/Penticton_Observed/monthly/MONTHLY.OBS.</p>

Climatic Indicators (5)

Global Mean Lan/Ocean Temperature

Values change over time!

Data values are in the file <http://data.giss.nasa.gov/gistemp/taledata/GLB.Ts+dSST.txt> from NASA/GISS. Please read and refer to this web page plus the main web page describing various temperature indices at <http://data.giss.nasa.gov/gistemp/>. Note, the index is an **anomaly** index. They have comments in the datafile and the writeup on obtaining an absolute global mean temperatures. Please reference the papers:

- Christy, J.R., R.W. Spencer, and W.D. Braswell 2000. J. Atmos. Oceanic Tech. 17, 1153.
- Hansen, J., R. Ruedy, M. Sato and R. Reynolds 1996. Global surface air temperature in 1995: Return to pre-Pinatubo level. Geophys. Res. Lett. 23, 1665-1668.
- Hansen, J., M. Sato, J. Glascoe and R. Ruedy 1998. A common-sense climate index: Is climate changing noticeably? Proc. Natl. Acad. Sci. 95, 4113-4120.
- Hansen, J., R. Ruedy, J. Glascoe, and M. Sato 1999. GISS analysis of surface temperature change. J. Geophys. Res. 104, 30997-31022.
- Hansen, J., R. Ruedy, M. Sato, M. Imhoff, W. Lawrence, D. Easterling, T. Peterson, and T. Karl 2001. A closer look at United States and global surface temperature change. J. Geophys. Res. 106, 23947-23963
- Intergovernmental Panel on Climate Change 2001. Climate Change 2001 (J.T. Houghton et al., Eds.), Cambridge Univ. Press, New York.
- National Research Council 2000. Reconciling Observations of Global Temperature Change. National Academy Press, Washington, DC, 85 pp.
- Peterson, T.C., and R.S. Vose 1997. An overview of the Global Historical Climatology Network temperature database. Bull. Amer. Meteorol. Soc. 78, 2837-2849.
- Rayner, N. 2000. HadISST1 Seaice and sea surface temperature files. Hadley Center, Bracknell, U.K.
- Reynolds, R.W., N.A. Rayner, T.M. Smith, D.C. Stokes, and W. Wang 2002. An improved in situ and satellite SST analysis for climate. J. Climate 15, 1609-1625, doi:10.1175/1520-0442(2002)015<1609:AIIASAS>2.0.CO;2.
- Reynolds, R.W., and T.M. Smith 1994. Improved global sea surface temperature analyses. J. Climate 7, 929-948, doi:10.1175/1520-0442(1994)007<0929:IGSSTA>2.0.CO;2
- Smith, T.M., R.W. Reynolds, R.E. Livesay, and D.C. Stokes 1996. Reconstruction of historical sea surface temperature using empirical orthogonal functions. J. Climate 9, 1403-1420.

Global Mean
Lan/Ocean
Temperature
Index

Source:

U.S. Department of Commerce | National Oceanic & Atmospheric Administration | NOAA Research



Earth System Research Laboratory
Physical Sciences Division

